

$\sqrt{4}$

2

MATRICES

EJERCICIO 1

INTRODUCIR UN TEXTO

$\sqrt{2}$.

1.41421

$N[\sqrt{2}, 200]$

1.4142135623730950488016887242096980785696718753769480731766797379907:
32478462107038850387534327641572735013846230912297024924836055850737:
2126441214970999358314132226659275055927557999505011527820605715

a := 3

b := 7

a + b

10

A := $\begin{pmatrix} -1 & 2 & 0 \\ 1 & 3 & -1 \\ 0 & 1 & 2 \end{pmatrix}$

B := $\begin{pmatrix} 0 & 1 & 3 \\ -1 & 4 & 5 \\ 2 & 1 & 3 \end{pmatrix}$

```
2 A - 5 B
```

```
{{-2, -1, -15}, {7, -14, -27}, {-10, -3, -11}}
```

```
MatrixForm[A.B]
```

```

$$\begin{pmatrix} -2 & 7 & 7 \\ -5 & 12 & 15 \\ 3 & 6 & 11 \end{pmatrix}$$

```

```
B.A
```

```
{{1, 6, 5}, {5, 15, 6}, {-1, 10, 5}}
```

```
A.B == B.A
```

```
False
```

```
Det[Inverse[A]]
```

```
-0.0909091
```

```
Inverse[A.B] == Inverse[B].Inverse[A]
```

```
True
```

```
Det[A.B] == Det[A] * Det[B]
```

```
True
```

```
Inverse[5 Transpose[A] - 3 Det[B] A]
```

```
{{-0.0130293, 0.00745425, 0.00293412},  
 {0.00435529, 0.00393651, 0.00154948},  
 {-0.00171432, -0.00154948, 0.0100284}}
```

EJERCICIO 2

```
Clear[A, B]
```

```
A :=  $\begin{pmatrix} 3 & 2 & -2 \\ 1 & 3 & -1 \\ 1 & 2 & 0 \end{pmatrix}$ 
```

```
Eigenvalues[A]
```

```
{3, 2, 1}
```

La matriz A será diagonalizable

```
B :=  $\begin{pmatrix} 2 & 1 & 0 \\ 0 & 1 & -1 \\ 0 & 2 & 4 \end{pmatrix}$ 
```

```
Eigenvalues[B]
```

```
{3, 2, 2}
```

```
Eigenvectors[B]
```

```
{{-1, -1, 2}, {1, 0, 0}, {0, 0, 0}}
```

La matriz B no es diagonalizable

```
Eigenvectors[A]
```

```
{{1, 1, 1}, {0, 1, 1}, {1, 0, 1}}
```

```
p = Transpose[Eigenvectors[A]]
```

```
{{1, 0, 1}, {1, 1, 0}, {1, 1, 1}}
```

```
d = Inverse[p].A.p
```

```
{{3, 0, 0}, {0, 2, 0}, {0, 0, 1}}
```

```
MatrixForm[d]
```

```

$$\begin{pmatrix} 3 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

```

EJERCICIO 3

```
A := 
$$\begin{pmatrix} 3 & -2 & 1 \\ 2 & -2 & 2 \\ 1 & -2 & -5 \end{pmatrix}$$

```

```
Eigenvalues[A]
```

```
{-4, -2, 2}
```

```
Eigenvectors[A]
```

```
{{-1, -2, 3}, {-1, -2, 1}, {2, 1, 0}}
```

```
p = Transpose[Eigenvectors[A]]
```

```
{{-1, -1, 2}, {-2, -2, 1}, {3, 1, 0}}
```

```
d = Inverse[p].A.p
```

```
{{-4, 0, 0}, {0, -2, 0}, {0, 0, 2}}
```

```
MatrixForm[d]
```

$$\begin{pmatrix} -4 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & 2 \end{pmatrix}$$

```
MatrixPower[A, 20]
```

```
{{183252811776, -366503526400, -549755289600},  
{366503526400, -733006004224, -1099510579200},  
{-549755289600, 1099510579200, 1649266917376}}
```

$$p \cdot \begin{pmatrix} 4^{20} & 0 & 0 \\ 0 & -2^{20} & 0 \\ 0 & 0 & 2^{20} \end{pmatrix} \cdot \text{Inverse}[p]$$

```
{{183253860352, -366505623552, -549756338176},  
{366505623552, -733010198528, -1099512676352},  
{-549756338176, 1099512676352, 1649267965952}}
```