

# Mathematics 1 - ADE/FyCo - 2020/2021

## List of exercises 03-Integration for identity number: 113

### Exercise 1

Compute  $\int_{3a}^3 (-15 - 51a + 34t + 60at - 30t^2 - 18at^2 + 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 5
- 2) 9
- 3) 0
- 4) The rest of the solutions are not correct
- 5) 6
- 6) -17

### Exercise 2

Compute  $\int_{-3}^3 ((6 + 6t) \cos[3 - 3t]) dt$

- 1) -5.80095
- 2) -3.49642
- 3) 35.613
- 4) -2.44829
- 5) -0.0114881
- 6) -2.84669

### Exercise 3

Compute  $\int_5^7 \left( \frac{128}{(-1 + 2t)^4} \right) dt$

- 1) -2.44829
- 2) 0.0195536
- 3) -2.33236
- 4) -104081.
- 5) -3.49642
- 6) -2.84669

## Exercise 4

Compute  $\int_4^7 \left( \frac{15 - 2a - 5t + at}{6 - 5t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
 Compute the derivative of such a formula at the point  $0$ .

- 1) 1.80569
- 2) 1.27419
- 3) 1.02439
- 4) The rest of the solutions are not correct
- 5) 1.50609
- 6) 0.806594

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function  $v(t) = 3 + 3t^2 + 2t^3 + 2t^4$  millions of euros/year.

If the initial deposit in the investment fund was 90 millions of euros, compute the deposits available after 2 years.

- 1)  $\frac{2637}{10}$  millions of euros = 263.7 millions of euros
- 2)  $\frac{3518}{5}$  millions of euros = 703.6 millions of euros
- 3)  $\frac{949}{10}$  millions of euros = 94.9 millions of euros
- 4)  $\frac{624}{5}$  millions of euros = 124.8 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (2 + t + 3t^2) \log(2t) \text{ euros.}$$

Compute the average value of shares between month 1 and month 3 (between  $t=1$  and  $t=3$ ).

- 1)  $\frac{1}{2} \left( -\frac{123}{4} - \frac{7 \log[2]}{2} + 80 \log[8] \right)$  euros = 66.5897 euros
- 2)  $\frac{1}{3} \left( -\frac{166}{3} - \frac{7 \log[2]}{2} + \frac{295 \log[10]}{2} \right)$  euros = 93.9573 euros
- 3)  $\frac{1}{2} \left( -\frac{44}{3} - \frac{7 \log[2]}{2} + \frac{75 \log[6]}{2} \right)$  euros = 25.0491 euros
- 4)  $\frac{1}{3} \left( -\frac{123}{4} - \frac{7 \log[2]}{2} + 80 \log[8] \right)$  euros = 44.3931 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 36 - 18x - 4x^2 + 2x^3$  and the horizontal axis between the points  $x = -2$  and  $x = 2$ .

1)  $\frac{757}{6} = 126.1667$

2)  $\frac{383}{3} = 127.6667$

3)  $\frac{374}{3} = 124.6667$

4)  $\frac{368}{3} = 122.6667$

5)  $\frac{380}{3} = 126.6667$

6)  $\frac{377}{3} = 125.6667$

7)  $\frac{392}{3} = 130.6667$

8)  $\frac{751}{6} = 125.1667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1}{100} (3 + 2t + t^2) \right) \log(t) \text{ per-unit.}$$

In the year  $t=1$  we deposit in the account 15000 euros. Compute the deposit in the account after (with respect to  $t=1$ ) 4 years.

1) 38289.2506 euros

2) 38329.2506 euros

3) 38269.2506 euros

4) 38359.2506 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

## List of exercises 03-Integration for identity number: 4501

## Exercise 1

$$\text{Compute } \int_a^{-4} (2 - 4a + 8t - 6at + 9t^2 - 3at^2 + 4t^3) dt$$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) 47
- 2) 20
- 3) The rest of the solutions are not correct
- 4) 30
- 5) 19
- 6) 27

## Exercise 2

$$\text{Compute } \int_{-2}^3 (-(4 - 2t) \sin[2 - 2t]) dt$$

- 1) -12.1631
- 2) -10.2796
- 3) -4.94292
- 4) 14.7752
- 5) -8.21561
- 6) -2.75011

## Exercise 3

$$\text{Compute } \int_4^8 \left( \frac{12}{(-5 + 2t)^2} \right) dt$$

- 1) -6.43314
- 2) -4.34527
- 3) 1.45455
- 4) -3.64908
- 5) -1304.
- 6) -5.43694

## Exercise 4

Compute  $\int_3^5 \left( \frac{-2a + 2t + at}{-2t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) -0.381974
- 2) 0.293426
- 3) 0.510826
- 4) The rest of the solutions are not correct
- 5) 0.406126
- 6) 0.551726

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 2 + 3t + 2t^2 + 2t^3 + 3t^4 \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 90 millions of euros, compute the deposits available after 1 year.

- 1)  $\frac{1569}{5}$  millions of euros = 313.8 millions of euros
- 2)  $\frac{13606}{15}$  millions of euros = 907.0667 millions of euros
- 3)  $\frac{1429}{15}$  millions of euros = 95.2667 millions of euros
- 4)  $\frac{1988}{15}$  millions of euros = 132.5333 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = (6 + t)e^{-1+3t} \text{ euros.}$$

Compute the average value of the shares along the first 3 months of the year (between t=0 and t=3).

- 1)  $\frac{1}{3} \left( -\frac{17}{9e} + \frac{20e^2}{9} \right)$  euros = 5.2417 euros
- 2)  $\frac{1}{3} \left( -\frac{17}{9e} + \frac{26e^8}{9} \right)$  euros = 2870.3205 euros
- 3)  $\frac{1}{3} \left( -\frac{17}{9e} + \frac{23e^5}{9} \right)$  euros = 126.1944 euros
- 4)  $\frac{1}{3} \left( \frac{14}{9e^4} - \frac{17}{9e} \right)$  euros = -0.2221 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 2x - x^2$  and the horizontal axis between the points  $x = -3$  and  $x = 0$ .

- 1)  $\frac{41}{2} = 20.5$
- 2)  $\frac{45}{2} = 22.5$
- 3) 20
- 4) 22
- 5) 18
- 6)  $\frac{43}{2} = 21.5$
- 7)  $\frac{39}{2} = 19.5$
- 8) 21

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{1}{8} (2 + 2t)\right) e^{-3+2t} \text{ per-unit.}$$

The initial deposit in the account is 15000 euros. Compute the deposit after 1 year.

- 1) 16021.249 euros
- 2) 16091.249 euros
- 3) 16101.249 euros
- 4) 16051.249 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 187462

#### Exercise 1

Compute  $\int_{-a}^{-3} (-4 - 9a - 18t + 15at^2 + 20t^3) dt$

- . The resulting expression is a formula in terms of parameter  
a. Compute the derivative of such a formula at the point 0.

- 1) -114
- 2) The rest of the solutions are not correct
- 3) -119
- 4) -104
- 5) -127
- 6) -117

#### Exercise 2

Compute  $\int_{-2}^2 (-e^{1+t}) dt$

- 1) -19.7177
- 2) -90.3239
- 3) -82.282
- 4) -95.803
- 5) -40.9068
- 6) -40.9068

#### Exercise 3

Compute  $\int_{-6}^{-2} \left( \frac{63}{(-4 + 3t)^2} \right) dt$

- 1) -5.56547
- 2) 1.14545
- 3) -4.77999
- 4) -5.24717
- 5) -4.7442
- 6) -9648.

## Exercise 4

Compute  $\int_2^3 \left( \frac{2 - 5a - 2t - 5at}{-1 + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2)  $-3.10354$
- 3)  $-3.58014$
- 4)  $-4.04204$
- 5)  $-3.66514$
- 6)  $-4.13744$

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (4 + 4t) \log(5t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were  $50$  millions euros, compute the deposit available after (with respect to  $t=1$ )  $2$  years.

- 1)  $23 - 6 \log[5] + 48 \log[20]$  millions of euros =  $157.1385$  millions of euros
- 2)  $10 - 6 \log[5] + 70 \log[25]$  millions of euros =  $225.6647$  millions of euros
- 3)  $54 - 6 \log[5] + 30 \log[15]$  millions of euros =  $125.5849$  millions of euros
- 4)  $34 - 6 \log[5] + 30 \log[15]$  millions of euros =  $105.5849$  millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (-4 + 3t) \cos(8t) \text{ euros.}$$

Compute the average value of the shares along the first  $2\pi$  months of the year (between  $t=0$  and  $t=2\pi$ ).

- 1)  $-70$  euros
- 2)  $10$  euros
- 3)  $0$  euros
- 4)  $30$  euros



## Exercise 7

Compute the area enclosed by the function  $f(x) = 6 - 3x - 6x^2 + 3x^3$  and the horizontal axis between the points  $x = -5$  and  $x = 2$ .

1)  $\frac{2661}{4} = 665.25$

2)  $\frac{2671}{4} = 667.75$

3)  $\frac{2651}{4} = 662.75$

4)  $\frac{2673}{4} = 668.25$

5)  $\frac{2597}{4} = 649.25$

6)  $\frac{2669}{4} = 667.25$

7)  $\frac{2587}{4} = 646.75$

8)  $\frac{2667}{4} = 666.75$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{1}{100}(-1 + 8t)\right) \cos(4t) \text{ per-unit.}$$

The initial deposit in the account is 11000 euros. Compute the deposit after  $2\pi$  years.

1) 11000 euros

2) 10940 euros

3) 11060 euros

4) 10910 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 550273

### Exercise 1

Compute  $\int_a^5 (3a - 6t + 8at - 12t^2 - 15at^2 + 20t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -513
- 2) -510
- 3) The rest of the solutions are not correct
- 4) -511
- 5) -505
- 6) -503

### Exercise 2

Compute  $\int_1^5 ((-4 + 4t) \text{Log}[2t]) dt$

- 1) 62.4638
- 2) 194.774
- 3) -173.278
- 4) -241.857
- 5) 70.4638
- 6) -169.36

### Exercise 3

Compute  $\int_1^7 \left( \frac{448}{(4 + 4t)^3} \right) dt$

- 1) -1.93318
- 2) -522240.
- 3) -3.87195
- 4) -2.77406
- 5) 0.820313
- 6) -2.71134

## Exercise 4

Compute  $\int_5^8 \left( \frac{5 - 9a - 5t + 3at}{3 - 4t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) 1.13155
- 3) 1.16815
- 4) 1.24745
- 5) 1.14395
- 6) 2.17615

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (4 + t)e^{2+t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 60 millions of euros, compute the deposits available after 3 years.

- 1)  $60 - 3e^2 + 4e^3$  millions of euros = 118.175 millions of euros
- 2)  $60 + 2e - 3e^2$  millions of euros = 43.2694 millions of euros
- 3)  $60 - 3e^2 + 6e^5$  millions of euros = 928.3118 millions of euros
- 4)  $60 - 3e^2 + 5e^4$  millions of euros = 310.8236 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (-7 - 6t) \cos(7t) \text{ euros.}$$

Compute the average value of the shares along the first  $\pi$  months of the year (between  $t=0$  and  $t=\pi$ ).

- 1) 0 euros
- 2)  $70 + \frac{12}{49\pi}$  euros = 70.078 euros
- 3)  $90 + \frac{12}{49\pi}$  euros = 90.078 euros
- 4)  $\frac{12}{49\pi}$  euros = 0.078 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -18 + 15x + 6x^2 - 3x^3$  and the horizontal axis between the points  $x = -2$  and  $x = 2$ .

- 1) 56
- 2)  $\frac{117}{2} = 58.5$
- 3)  $\frac{113}{2} = 56.5$
- 4)  $\frac{115}{2} = 57.5$
- 5) 57
- 6) 40
- 7)  $\frac{109}{2} = 54.5$
- 8) 58

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1}{100} (-3 - 5t) \right) \cos(7t) \text{ per-unit.}$$

The initial deposit in the account is 9000 euros. Compute the deposit after  $5\pi$  years.

- 1) 9108.3861 euros
- 2) 9088.3861 euros
- 3) 9018.3861 euros
- 4) 8988.3861 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 2959749

### Exercise 1

Compute  $\int_a^{-5} (-4 - a + 2t - 2at + 3t^2 + 12at^2 - 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2)  $-530$
- 3)  $-532$
- 4)  $-516$
- 5)  $-533$
- 6)  $-529$

### Exercise 2

Compute  $\int_0^1 (e^{1-t} (3 - 3t - 2t^2)) dt$

- 1)  $-8.73151$
- 2)  $-10.6212$
- 3)  $0.833333$
- 4)  $2.12687$
- 5)  $-0.833333$
- 6)  $-9.26058$

### Exercise 3

Compute  $\int_{-6}^3 \left(\frac{2}{t^5}\right) dt$

- 1)  $11481.8$
- 2)  $-0.00578704$
- 3)  $-4.10533$
- 4)  $-4.99382$
- 5)  $-4.35408$
- 6)  $-3.48321$

## Exercise 4

Compute  $\int_0^1 \left( \frac{5 + 10a + 5t + 5at}{2 + 3t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter a.  
Compute the derivative of such a formula at the point 0.

- 1) 3.31864
- 2) The rest of the solutions are not correct
- 3) 2.47784
- 4) 2.82494
- 5) 3.13554
- 6) 3.46574

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (1+t) \log(4t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 60 millions euros, compute the deposit available after (with respect to  $t=1$ ) 4 years.

- 1)  $50 - \frac{3 \operatorname{Log}[4]}{2} + \frac{35 \operatorname{Log}[20]}{2}$  millions of euros = 100.3459 millions of euros
- 2)  $\frac{213}{4} - \frac{3 \operatorname{Log}[4]}{2} + 12 \operatorname{Log}[16]$  millions of euros = 84.4416 millions of euros
- 3)  $90 - \frac{3 \operatorname{Log}[4]}{2} + \frac{35 \operatorname{Log}[20]}{2}$  millions of euros = 140.3459 millions of euros
- 4)  $\frac{185}{4} - \frac{3 \operatorname{Log}[4]}{2} + 24 \operatorname{Log}[24]$  millions of euros = 120.4439 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = \cos(-3 + 9t) \text{ euros.}$$

Compute the average value of the shares along the first  $3\pi$  months of the year (between  $t=0$  and  $t=3\pi$ ).

- 1)  $\frac{2 \operatorname{Sin}[3]}{27\pi}$  euros = 0.0033 euros
- 2)  $50 + \frac{2 \operatorname{Sin}[3]}{27\pi}$  euros = 50.0033 euros
- 3)  $-60 + \frac{2 \operatorname{Sin}[3]}{27\pi}$  euros = -59.9967 euros
- 4)  $-80 + \frac{2 \operatorname{Sin}[3]}{27\pi}$  euros = -79.9967 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -12 - 12x + 3x^2 + 3x^3$  and the horizontal axis between the points  $x = -5$  and  $x = 2$ .

$$1) \frac{1127}{4} = 281.75$$

$$2) \frac{1141}{4} = 285.25$$

$$3) \frac{1151}{4} = 287.75$$

$$4) \frac{871}{4} = 217.75$$

$$5) \frac{857}{4} = 214.25$$

$$6) \frac{1155}{4} = 288.75$$

$$7) \frac{1149}{4} = 287.25$$

$$8) \frac{1153}{4} = 288.25$$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \cos(-3 + t) \text{ per-unit.}$$

The initial deposit in the account is 8000 euros. Compute the deposit after  $3\pi$  years.

$$1) 8189.0086 \text{ euros}$$

$$2) 8229.0086 \text{ euros}$$

$$3) 8169.0086 \text{ euros}$$

$$4) 8199.0086 \text{ euros}$$

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 3180328

### Exercise 1

Compute  $\int_a^1 (-1 - 4a + 8t - 6at + 9t^2 + 6at^2 - 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -7
- 2) -10
- 3) -4
- 4) The rest of the solutions are not correct
- 5) -18
- 6) -5

### Exercise 2

Compute  $\int_3^6 (-2 \text{Log}[t]) dt$

- 1) -14.9094
- 2) -8.90944
- 3) -55.2317
- 4) -40.671
- 5) -38.4833
- 6) -42.0945

### Exercise 3

Compute  $\int_{-9}^6 \left( \frac{4\theta}{(3 + 2t)^3} \right) dt$

- 1) -4.7247
- 2) -3.88617
- 3) -4.56493
- 4) -0.0790123
- 5) 22032.
- 6) -4.31938



## Exercise 4

Compute  $\int_4^6 \left( \frac{-6a + 5t + 2at}{-3t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter a.  
Compute the derivative of such a formula at the point 0.

- 1) 1.03823
- 2) 0.88573
- 3) The rest of the solutions are not correct
- 4) 0.81093
- 5) 1.00223
- 6) 0.98673

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function  $v(t) = 20e^{3+t}$  millions of euros/year.

If the initial deposit in the investment fund was 90 millions of euros, compute the deposits available after 3 years.

- 1)  $90 - 20e^3 + 20e^4$  millions of euros = 780.2523 millions of euros
- 2)  $90 + 20e^2 - 20e^3$  millions of euros = -163.9296 millions of euros
- 3)  $90 - 20e^3 + 20e^5$  millions of euros = 2656.5524 millions of euros
- 4)  $90 - 20e^3 + 20e^6$  millions of euros = 7756.8651 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = (9 + 8t)e^{2+2t} \text{ euros.}$$

Compute the average value of the shares along the first 9 months of the year (between  $t=0$  and  $t=9$ ).

- 1)  $\frac{1}{9} \left( -\frac{5e^2}{2} + \frac{77e^{20}}{2} \right)$  euros =  $2.0754 \times 10^9$  euros
- 2)  $\frac{1}{9} \left( -\frac{5e^2}{2} + \frac{13e^4}{2} \right)$  euros = 37.3795 euros
- 3)  $\frac{1}{9} \left( -\frac{3}{2} - \frac{5e^2}{2} \right)$  euros = -2.2192 euros
- 4)  $\frac{1}{9} \left( -\frac{5e^2}{2} + \frac{21e^6}{2} \right)$  euros = 468.6144 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -9x - 6x^2 + 3x^3$  and the horizontal axis between the points  $x=1$  and  $x=5$ .

- 1) 168
- 2)  $\frac{343}{2} = 171.5$
- 3) 112
- 4) 172
- 5)  $\frac{339}{2} = 169.5$
- 6)  $\frac{341}{2} = 170.5$
- 7) 170
- 8) 171

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{-2+t}{1628} \right) e^{2+3t} \text{ per-unit.}$$

The initial deposit in the account is 7000 euros. Compute the deposit after 1 year.

- 1) 6765.8226 euros
- 2) 6725.8226 euros
- 3) 6835.8226 euros
- 4) 6745.8226 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 6548030

#### Exercise 1

Compute  $\int_{3a}^{\theta} (9a - 6t - 24at + 12t^2 - 27at^2 + 12t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -4
- 2) -8
- 3) 0
- 4) -20
- 5) The rest of the solutions are not correct
- 6) -14

#### Exercise 2

Compute  $\int_2^3 ((-1 - 3t) \cos[1 + t]) dt$

- 1) -34.9675
- 2) -34.9442
- 3) 7.54682
- 4) 13.6162
- 5) 2.86518
- 6) -35.5057

#### Exercise 3

Compute  $\int_{-9}^3 \left( \frac{96}{(1 + 4t)^2} \right) dt$

- 1) -41544.
- 2) -6.85058
- 3) -6.92744
- 4) -7.03876
- 5) -6.93207
- 6) 1.4961

## Exercise 4

Compute  $\int_2^3 \left( \frac{-3 + 15a + 3t + 5at}{-3 + 2t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) 4.13754
- 2) 2.96524
- 3) The rest of the solutions are not correct
- 4) 3.46574
- 5) 2.49244
- 6) 3.69634

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (1 + 4t + t^2) \log(3t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 80 millions euros, compute the deposit available after (with respect to  $t=1$ ) 3 years.

- 1)  $\frac{145}{9} - \frac{10 \log[3]}{3} + 150 \log[18]$  millions of euros = 446.0048 millions of euros
- 2)  $\frac{344}{9} - \frac{10 \log[3]}{3} + \frac{290 \log[15]}{3}$  millions of euros = 296.3384 millions of euros
- 3)  $55 - \frac{10 \log[3]}{3} + \frac{172 \log[12]}{3}$  millions of euros = 193.8059 millions of euros
- 4)  $45 - \frac{10 \log[3]}{3} + \frac{172 \log[12]}{3}$  millions of euros = 183.8059 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (-7 - 5t) \cos(9t) \text{ euros.}$$

Compute the average value of the shares along the first  $3\pi$  months of the year (between  $t=0$  and  $t=3\pi$ ).

- 1) 0 euros
- 2)  $\frac{10}{243\pi}$  euros = 0.0131 euros
- 3)  $-90 + \frac{10}{243\pi}$  euros = -89.9869 euros
- 4)  $50 + \frac{10}{243\pi}$  euros = 50.0131 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -18 + 18x + 2x^2 - 2x^3$  and the horizontal axis between the points  $x = -3$  and  $x = 1$ .

1)  $\frac{521}{6} = 86.8333$

2)  $\frac{533}{6} = 88.8333$

3)  $\frac{265}{3} = 88.3333$

4)  $\frac{268}{3} = 89.3333$

5)  $\frac{256}{3} = 85.3333$

6)  $\frac{527}{6} = 87.8333$

7)  $\frac{539}{6} = 89.8333$

8)  $\frac{262}{3} = 87.3333$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{1}{100}(-1 - 7t)\right) \cos(3t) \text{ per-unit.}$$

The initial deposit in the account is 18000 euros. Compute the deposit after  $5\pi$  years.

1) 18312.1891 euros

2) 18292.1891 euros

3) 18282.1891 euros

4) 18222.1891 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 7476889

### Exercise 1

Compute  $\int_{-3a}^{-4} (10 - 27a - 18t + 36at + 18t^2 - 18at^2 - 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 805
- 2) The rest of the solutions are not correct
- 3) 810
- 4) 809
- 5) 811
- 6) 825

### Exercise 2

Compute  $\int_0^1 (-(9 - 27t - 27t^2) \sin[2 - 3t]) dt$

- 1) -22.8435
- 2) -19.447
- 3) 2.43136
- 4) -22.5668
- 5) -11.3599
- 6) -5.35794

### Exercise 3

Compute  $\int_0^5 \left(-\frac{64}{(-5 - 2t)^5}\right) dt$

- 1) -3.62357
- 2)  $-2.84375 \times 10^6$
- 3) -3.62957
- 4) -4.21184
- 5) 0.012642
- 6) -4.26349

## Exercise 4

Compute  $\int_7^8 \left( \frac{-6 - 15a + 2t - 5at}{-9 + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) -1.37062
- 2) -1.45172
- 3) -2.04852
- 4) -1.54482
- 5) The rest of the solutions are not correct
- 6) -1.57132

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (2 + t) \log(2t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 50 millions euros, compute the deposit available after (with respect to  $t=1$ ) 2 years.

- 1)  $44 - \frac{5 \operatorname{Log}[2]}{2} + \frac{21 \operatorname{Log}[6]}{2}$  millions of euros = 61.0806 millions of euros
- 2)  $36 - \frac{5 \operatorname{Log}[2]}{2} + \frac{45 \operatorname{Log}[10]}{2}$  millions of euros = 86.0753 millions of euros
- 3)  $134 - \frac{5 \operatorname{Log}[2]}{2} + \frac{21 \operatorname{Log}[6]}{2}$  millions of euros = 151.0806 millions of euros
- 4)  $\frac{161}{4} - \frac{5 \operatorname{Log}[2]}{2} + 16 \operatorname{Log}[8]$  millions of euros = 71.7882 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (4 + 2t + 4t^2) \log(5t) \text{ euros.}$$

Compute the average value of shares between month 1 and month 3 (between  $t=1$  and  $t=3$ ).

- 1)  $\frac{1}{3} \left( -\frac{95}{2} - \frac{19 \operatorname{Log}[5]}{3} + \frac{352 \operatorname{Log}[20]}{3} \right)$  euros = 97.9354 euros
- 2)  $\frac{1}{2} \left( -\frac{95}{2} - \frac{19 \operatorname{Log}[5]}{3} + \frac{352 \operatorname{Log}[20]}{3} \right)$  euros = 146.9031 euros
- 3)  $\frac{1}{3} \left( -\frac{748}{9} - \frac{19 \operatorname{Log}[5]}{3} + \frac{635 \operatorname{Log}[25]}{3} \right)$  euros = 196.0082 euros
- 4)  $\frac{1}{2} \left( -\frac{212}{9} - \frac{19 \operatorname{Log}[5]}{3} + 57 \operatorname{Log}[15] \right)$  euros = 60.3051 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -9x + x^3$  and the horizontal axis between the points  $x=0$  and  $x=3$ .

1)  $\frac{93}{4} = 23.25$

2)  $\frac{91}{4} = 22.75$

3)  $\frac{89}{4} = 22.25$

4)  $\frac{81}{4} = 20.25$

5)  $\frac{95}{4} = 23.75$

6)  $\frac{97}{4} = 24.25$

7)  $\frac{87}{4} = 21.75$

8)  $\frac{99}{4} = 24.75$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{2+t}{100}\right) \log(2t) \text{ per-unit.}$$

In the year  $t=1$  we deposit in the account 4000 euros. Compute the deposit in the account after (with respect to  $t=1$ ) 4 years.

1) 5737.6363 euros

2) 5787.6363 euros

3) 5817.6363 euros

4) 5797.6363 euros



## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 7511947

#### Exercise 1

Compute  $\int_{-a}^4 (1 - 3a - 6t + 8at + 12t^2 - 6at^2 - 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) -84
- 2) The rest of the solutions are not correct
- 3) -71
- 4) -66
- 5) -75
- 6) -67

#### Exercise 2

Compute  $\int_{-2}^2 (-\cos[1 - 3t]) dt$

- 1) 1.07727
- 2) -2.17527
- 3) -4.37025
- 4) -2.07513
- 5) 0.100646
- 6) -3.3991

#### Exercise 3

Compute  $\int_{-4}^{-1} \left( \frac{1250}{(2 - 5t)^4} \right) dt$

- 1) -4.37025
- 2) -1.84491
- 3) -3.3991
- 4) -2.17527
- 5)  $1.71228 \times 10^6$
- 6) 0.235128

## Exercise 4

Compute  $\int_3^4 \left( \frac{15 + 5t + 2at}{3t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) -0.200499
- 2) -0.683699
- 3) -0.0340986
- 4) -0.0900986
- 5) The rest of the solutions are not correct
- 6) 0.308301

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 10e^{-1+2t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 20 millions of euros, compute the deposits available after 1 year.

- 1)  $20 + \frac{5}{e^3} - \frac{5}{e}$  millions of euros = 18.4095 millions of euros
- 2)  $20 - \frac{5}{e} + 5e$  millions of euros = 31.752 millions of euros
- 3)  $20 - \frac{5}{e} + 5e^3$  millions of euros = 118.5883 millions of euros
- 4)  $20 - \frac{5}{e} + 5e^5$  millions of euros = 760.2264 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = 3 + 2t + 3t^2 + 3t^3 + t^4 \text{ euros.}$$

Compute the average value of the shares along the first 4 months of the year (between t=0 and t=4).

- 1)  $\frac{611}{5}$  euros = 122.2 euros
- 2)  $\frac{3087}{80}$  euros = 38.5875 euros
- 3)  $\frac{91}{10}$  euros = 9.1 euros
- 4)  $\frac{119}{80}$  euros = 1.4875 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -6x - 2x^2$  and the horizontal axis between the points  $x=1$  and  $x=4$ .

- 1)  $\frac{177}{2} = 88.5$
- 2) 87
- 3) 92
- 4) 89
- 5)  $\frac{183}{2} = 91.5$
- 6)  $\frac{179}{2} = 89.5$
- 7) 91
- 8) 90

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{100} (3 + 2t + 3t^2 + 3t^3) \text{ per-unit.}$$

The initial deposit in the account is 14000 euros. Compute the deposit after 1 year.

- 1) 14828.5938 euros
- 2) 14868.5938 euros
- 3) 14818.5938 euros
- 4) 14898.5938 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 7803104

#### Exercise 1

Compute  $\int_{-3a}^2 (18a + 12t - 66at - 33t^2 + 36at^2 + 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 6
- 2) 0
- 3) 8
- 4) 5
- 5) The rest of the solutions are not correct
- 6) -11

#### Exercise 2

Compute  $\int_{-1}^1 (e^{3+t} (-1 - 2t)) dt$

- 1) -109.196
- 2) -337.575
- 3) -109.196
- 4) -76.7653
- 5) -338.858
- 6) -352.745

#### Exercise 3

Compute  $\int_{-2}^0 \left( \frac{135}{(-2 + 3t)^3} \right) dt$

- 1) -24.232
- 2) -5.27344
- 3) -23.278
- 4) -21.2668
- 5) -23.1899
- 6) 2040.

## Exercise 4

Compute  $\int_2^3 \left( \frac{-3 + 3t - 4at}{-t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) -2.77259
- 2) The rest of the solutions are not correct
- 3) -2.05849
- 4) -2.21349
- 5) -2.46739
- 6) -3.09459

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (9 + 8t)(\cos(2\pi t) + 1) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 40 millions of euros, compute the deposits available after 3 years.

- 1) 74 millions of euros
- 2) 103 millions of euros
- 3) 35 millions of euros
- 4) 53 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (5 - 7t) \cos(4t) \text{ euros.}$$

Compute the average value of the shares along the first  $2\pi$  months of the year (between  $t=0$  and  $t=2\pi$ ).

- 1) 30 euros
- 2) -30 euros
- 3) -80 euros
- 4) 0 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -2x + x^2 + x^3$  and the horizontal axis between the points  $x=-2$  and  $x=5$ .

$$1) \frac{2147}{12} = 178.9167$$

$$2) \frac{681}{4} = 170.25$$

$$3) \frac{2153}{12} = 179.4167$$

$$4) \frac{2159}{12} = 179.9167$$

$$5) \frac{2165}{12} = 180.4167$$

$$6) \frac{2117}{12} = 176.4167$$

$$7) \frac{2135}{12} = 177.9167$$

$$8) \frac{2141}{12} = 178.4167$$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1}{100} (-8 - t) \right) \cos(6t) \text{ per-unit.}$$

The initial deposit in the account is 13000 euros. Compute the deposit after  $5\pi$  years.

$$1) 12940 \text{ euros}$$

$$2) 12960 \text{ euros}$$

$$3) 13000 \text{ euros}$$

$$4) 13010 \text{ euros}$$

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 8623226

#### Exercise 1

Compute  $\int_a^{-2} (2a - 4t + 6at - 9t^2 - 15at^2 + 20t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) 55
- 3) 40
- 4) 29
- 5) 36
- 6) 48

#### Exercise 2

Compute  $\int_0^2 ((6 - 2t) \cos[2 + 2t]) dt$

- 1) -1.11766
- 2) -12.5985
- 3) -14.3822
- 4) -3.69547
- 5) 7.68136
- 6) -12.6968

#### Exercise 3

Compute  $\int_{-8}^3 \left( \frac{128}{(2 + 2t)^5} \right) dt$

- 1) -3.43579
- 2) -3.40918
- 3)  $1.88136 \times 10^6$
- 4) -3.20991
- 5) -3.89184
- 6) -0.0620835

## Exercise 4

Compute  $\int_1^3 \left( \frac{4 - 2a + 2t - 2at}{2 + 3t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1)  $-1.14125$
- 2)  $-0.945151$
- 3)  $-0.947351$
- 4) The rest of the solutions are not correct
- 5)  $-1.57415$
- 6)  $-1.02165$

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function  $v(t) = 20e^{2+3t}$  millions of euros/year.

If the initial deposit in the investment fund was 90 millions of euros, compute the deposits available after 3 years.

- 1)  $90 - \frac{20e^2}{3} + \frac{20e^5}{3}$  millions of euros = 1030.1607 millions of euros
- 2)  $90 - \frac{20e^2}{3} + \frac{20e^{11}}{3}$  millions of euros = 399201.6844 millions of euros
- 3)  $90 - \frac{20e^2}{3} + \frac{20e^8}{3}$  millions of euros = 19913.7929 millions of euros
- 4)  $90 + \frac{20}{3e} - \frac{20e^2}{3}$  millions of euros = 43.1922 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 30e^{3+3t} \text{ euros.}$$

Compute the average value of the shares along the first 4 months of the year (between  $t=0$  and  $t=4$ ).

- 1)  $\frac{1}{4} (-10e^3 + 10e^6)$  euros = 958.3581 euros
- 2)  $\frac{1}{4} (-10e^3 + 10e^{15})$  euros =  $8.1725 \times 10^6$  euros
- 3)  $\frac{1}{4} (10 - 10e^3)$  euros =  $-47.7138$  euros
- 4)  $\frac{1}{4} (-10e^3 + 10e^9)$  euros = 20207.496 euros



## Exercise 7

Compute the area enclosed by the function  $f(x) = 4 + 6x + 2x^2$  and the horizontal axis between the points  $x=1$  and  $x=5$ .

1)  $\frac{524}{3} = 174.6667$

2)  $\frac{512}{3} = 170.6667$

3)  $\frac{527}{3} = 175.6667$

4)  $\frac{1051}{6} = 175.1667$

5)  $\frac{518}{3} = 172.6667$

6)  $\frac{1033}{6} = 172.1667$

7)  $\frac{1039}{6} = 173.1667$

8)  $\frac{521}{3} = 173.6667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{e^{-1+t}}{15} \text{ per-unit.}$$

The initial deposit in the account is 11000 euros. Compute the deposit after 1 year.

1) 11543.4612 euros

2) 11473.4612 euros

3) 11503.4612 euros

4) 11463.4612 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 8792788

## Exercise 1

Compute  $\int_{-3a}^{\theta} (6 - 33a - 22t - 72at - 36t^2 + 45at^2 + 20t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) 10
- 2) 27
- 3) 0
- 4) -2
- 5) 18
- 6) The rest of the solutions are not correct

## Exercise 2

Compute  $\int_1^3 ((-4 - 2t) \cos[2 - 2t]) dt$

- 1) -20.9888
- 2) 7.94643
- 3) 4.61083
- 4) -21.9565
- 5) -22.6046
- 6) 18.7265

## Exercise 3

Compute  $\int_{-7}^{-2} \left( \frac{81}{(1 - 3t)^4} \right) dt$

- 1) 0.0253938
- 2) -4.76194
- 3) -4.08155
- 4) -4.55205
- 5) -4.9025
- 6)  $1.71228 \times 10^6$

## Exercise 4

Compute  $\int_2^3 \left( \frac{2+t+5at}{2t+t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) The rest of the solutions are not correct
- 2) 1.09622
- 3) 0.734018
- 4) 0.565118
- 5) 1.11572
- 6) 1.02362

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$v(t) = (1+t+4t^2) \log(2t)$  millions of euros/year.

If, for  $t=1$ , the deposits in the investment fund were 40 millions euros, compute the deposit available after (with respect to  $t=1$ ) 4 years.

- 1)  $-\frac{2495}{36} - \frac{17 \log[2]}{6} + 312 \log[12]$  millions of euros = 704.0214 millions of euros
- 2)  $-\frac{226}{9} - \frac{17 \log[2]}{6} + \frac{1105 \log[10]}{6}$  millions of euros = 396.9844 millions of euros
- 3)  $\frac{314}{9} - \frac{17 \log[2]}{6} + \frac{1105 \log[10]}{6}$  millions of euros = 456.9844 millions of euros
- 4)  $\frac{21}{4} - \frac{17 \log[2]}{6} + \frac{292 \log[8]}{3}$  millions of euros = 205.6851 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$V(t) = 30 e^{3+3t}$  euros.

Compute the average value of the shares along the first 8 months of the year (between  $t=0$  and  $t=8$ ).

- 1)  $\frac{1}{8} (10 - 10 e^3)$  euros = -23.8569 euros
- 2)  $\frac{1}{8} (-10 e^3 + 10 e^{27})$  euros =  $6.6506 \times 10^{11}$  euros
- 3)  $\frac{1}{8} (-10 e^3 + 10 e^9)$  euros = 10103.748 euros
- 4)  $\frac{1}{8} (-10 e^3 + 10 e^6)$  euros = 479.1791 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -4x - 6x^2 - 2x^3$  and the horizontal axis between the points  $x = -4$  and  $x = -1$ .

1)  $\frac{75}{2} = 37.5$

2)  $\frac{77}{2} = 38.5$

3)  $\frac{69}{2} = 34.5$

4) 35

5)  $\frac{65}{2} = 32.5$

6) 36

7)  $\frac{71}{2} = 35.5$

8)  $\frac{73}{2} = 36.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{14} e^{-6+2t} \text{ per-unit.}$$

The initial deposit in the account is 14000 euros. Compute the deposit after 3 years.

1) 14507.7514 euros

2) 14508.9857 euros

3) 14497.7514 euros

4) 14517.7514 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 9214549

#### Exercise 1

Compute  $\int_{-3a}^3 (-15 - 60a - 40t + 42at + 21t^2 + 36at^2 + 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 277
- 2) The rest of the solutions are not correct
- 3) 284
- 4) 278
- 5) 288
- 6) 270


#### Exercise 2

Compute  $\int_{-1}^0 (-2 \cos[3 + 2t]) dt$

- 1) -4.05317
- 2) -4.56856
- 3) 0.700351
- 4) -1.0806
- 5) -0.841471
- 6) -4.24482

#### Exercise 3

Compute  $\int_{-8}^{-2} \left(-\frac{3}{-1-3t}\right) dt$

 N: Internal precision limit \$MaxExtraPrecision = 50.` reached while evaluating  $\text{Log}\left[\frac{23}{5}\right] + \text{Log}[5] - \text{Log}[23]$ .

- 1) -4.32298
- 2) -6.97188
- 3) -6.18536
- 4) -5.23848
- 5) -6.47783
- 6) -1.52606

## Exercise 4

Compute  $\int_1^2 \left( \frac{2+t+at}{2t+t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) -0.577818
- 2) 0.209982
- 3) The rest of the solutions are not correct
- 4) -0.435518
- 5) 0.211482
- 6) 0.287682

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 2 + 3t + t^3 \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 40 millions of euros, compute the deposits available after 1 year.

- 1)  $\frac{175}{4}$  millions of euros = 43.75 millions of euros
- 2) 136 millions of euros
- 3)  $\frac{319}{4}$  millions of euros = 79.75 millions of euros
- 4) 54 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = 10 e^{-1+2t} \text{ euros.}$$

Compute the average value of the shares along the first 8 months of the year (between t=0 and t=8).

- 1)  $\frac{1}{8} \left( -\frac{5}{e} + 5 e^3 \right)$  euros = 12.3235 euros
- 2)  $\frac{1}{8} \left( -\frac{5}{e} + 5 e^{15} \right)$  euros =  $2.0431 \times 10^6$  euros
- 3)  $\frac{1}{8} \left( \frac{5}{e^3} - \frac{5}{e} \right)$  euros = -0.1988 euros
- 4)  $\frac{1}{8} \left( -\frac{5}{e} + 5 e \right)$  euros = 1.469 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -4x - 6x^2 - 2x^3$  and the horizontal axis between the points  $x = -2$  and  $x = 3$ .

- 1) 115
- 2) 116
- 3)  $\frac{233}{2} = 116.5$
- 4)  $\frac{231}{2} = 115.5$
- 5)  $\frac{235}{2} = 117.5$
- 6)  $\frac{227}{2} = 113.5$
- 7) 117
- 8)  $\frac{223}{2} = 111.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{8} e^{-9+3t} \text{ per-unit.}$$

The initial deposit in the account is 6000 euros. Compute the deposit after 3 years.

- 1) 6305.2493 euros
- 2) 6255.2493 euros
- 3) 6235.2493 euros
- 4) 6295.2493 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 9810258

### Exercise 1

Compute  $\int_{2a}^{-5} (15 + 20a - 20t + 80at - 60t^2 + 30at^2 - 20t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) -375
- 2) -367
- 3) -398
- 4) -372
- 5) -380
- 6) The rest of the solutions are not correct

### Exercise 2

Compute  $\int_0^1 (e^{-t} (3 - 3t + 2t^2)) dt$

- 1) -5.38867
- 2) -4.72792
- 3) 1.42484
- 4) -4.93779
- 5) -0.797072
- 6) -5.31616

### Exercise 3

Compute  $\int_{-8}^{-7} \left(-\frac{7}{-5-t}\right) dt$

- 1) -0.405465
- 2) -9.83597
- 3) -9.4179
- 4) -2.83826
- 5) -10.5897
- 6) -10.7341



## Exercise 4

Compute  $\int_3^4 \left( \frac{4 - 8a + 4t + 4at}{-2 - t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter a.  
Compute the derivative of such a formula at the point 0.

- 1) 1.15857
- 2) 1.11567
- 3) 0.274774
- 4) 0.892574
- 5) The rest of the solutions are not correct
- 6) 0.744874

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (6 + 7t)(\sin(2\pi t) + 1) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 70 millions of euros, compute the deposits available after 4 years.

- 1)  $\frac{135}{2} + \frac{7}{2\pi}$  millions of euros = 68.6141 millions of euros
- 2)  $\frac{159}{2} - \frac{7}{2\pi}$  millions of euros = 78.3859 millions of euros
- 3)  $150 - \frac{14}{\pi}$  millions of euros = 145.5437 millions of euros
- 4)  $96 - \frac{7}{\pi}$  millions of euros = 93.7718 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = \sin(4 + 4t) \text{ euros.}$$

Compute the average value of the shares along the first  $3\pi$  months of the year (between  $t=0$  and  $t=3\pi$ ).

- 1)  $20 + \frac{\frac{\cos[4]}{4} - \frac{1}{4} \cos[4(1 + 3\pi)]}{3\pi}$  euros = 20. euros
- 2)  $\frac{\frac{\cos[4]}{4} - \frac{1}{4} \cos[4(1 + 3\pi)]}{3\pi}$  euros = 0. euros
- 3)  $-30 + \frac{\frac{\cos[4]}{4} - \frac{1}{4} \cos[4(1 + 3\pi)]}{3\pi}$  euros = -30. euros
- 4)  $50 + \frac{\frac{\cos[4]}{4} - \frac{1}{4} \cos[4(1 + 3\pi)]}{3\pi}$  euros = 50. euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -4 - 2x + 2x^2$  and the horizontal axis between the points  $x = -5$  and  $x = 0$ .

- 1)  $\frac{193}{2} = 96.5$
- 2) 96
- 3)  $\frac{265}{3} = 88.3333$
- 4) 98
- 5) 97
- 6)  $\frac{191}{2} = 95.5$
- 7) 93
- 8) 95

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \sin(-3 + 6t) \text{ per-unit.}$$

The initial deposit in the account is 9000 euros. Compute the deposit after  $3\pi$  years.

- 1) 9080 euros
- 2) 9000 euros
- 3) 9090 euros
- 4) 9020 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 12865294

### Exercise 1

Compute  $\int_{3a}^{-1} (3a - 2t + 24at - 12t^2 + 27at^2 - 12t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\emptyset$ .

- 1)  $-2\emptyset$
- 2)  $-19$
- 3) The rest of the solutions are not correct
- 4)  $-12$
- 5)  $\emptyset$
- 6)  $-16$

### Exercise 2

Compute  $\int_{-2}^3 ((3-t) \cos[1+t]) dt$

- 1)  $-10.1374$
- 2)  $-15.3907$
- 3)  $1.38102$
- 4)  $5.4013$
- 5)  $-19.766$
- 6)  $-14.2722$

### Exercise 3

Compute  $\int_7^8 \left( \frac{6}{(2-t)^2} \right) dt$

- 1)  $-2.52812$
- 2)  $-2.84944$
- 3)  $-2.64236$
- 4)  $91.$
- 5)  $-3.65949$
- 6)  $0.2$

## Exercise 4

Compute  $\int_5^7 \left( \frac{4 + 9a + 4t - 3at}{-3 - 2t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) -1.59785
- 2) The rest of the solutions are not correct
- 3) -1.38325
- 4) -1.86115
- 5) -1.72615
- 6) -0.863046

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (9 + 8t)e^{-1+3t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 60 millions of euros, compute the deposits available after 2 years.

- 1)  $60 - \frac{19}{9e} + \frac{67e^5}{9}$  millions of euros = 1164.0769 millions of euros
- 2)  $60 - \frac{19}{9e} + \frac{91e^8}{9}$  millions of euros = 30200.0208 millions of euros
- 3)  $60 - \frac{19}{9e} + \frac{43e^2}{9}$  millions of euros = 94.5266 millions of euros
- 4)  $60 - \frac{5}{9e^4} - \frac{19}{9e}$  millions of euros = 59.2132 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = \cos(5 + 5t) \text{ euros.}$$

Compute the average value of the shares along the first  $\pi$  months of the year (between  $t=0$  and  $t=\pi$ ).

- 1)  $60 + \frac{-\frac{\sin[5]}{5} + \frac{1}{5} \sin[5(1+\pi)]}{\pi}$  euros = 60.1221 euros
- 2)  $90 + \frac{-\frac{\sin[5]}{5} + \frac{1}{5} \sin[5(1+\pi)]}{\pi}$  euros = 90.1221 euros
- 3)  $\frac{-\frac{\sin[5]}{5} + \frac{1}{5} \sin[5(1+\pi)]}{\pi}$  euros = 0.1221 euros
- 4)  $30 + \frac{-\frac{\sin[5]}{5} + \frac{1}{5} \sin[5(1+\pi)]}{\pi}$  euros = 30.1221 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -12 - 14x + 2x^3$  and the horizontal axis between the points  $x = -3$  and  $x = 2$ .

1)  $\frac{125}{2} = 62.5$

2) 63

3)  $\frac{121}{2} = 60.5$

4)  $\frac{115}{2} = 57.5$

5)  $\frac{83}{2} = 41.5$

6)  $\frac{127}{2} = 63.5$

7) 62

8)  $\frac{77}{2} = 38.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \cos(6 + 4t) \text{ per-unit.}$$

The initial deposit in the account is 12000 euros. Compute the deposit after  $2\pi$  years.

1) 12000 euros

2) 11930 euros

3) 12040 euros

4) 11920 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

## List of exercises 03-Integration for identity number: 13082921

## Exercise 1

Compute  $\int_{2a}^5 (-8 - 8a + 8t + 8at - 6t^2 - 6at^2 + 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -188
- 2) -174
- 3) The rest of the solutions are not correct
- 4) -185
- 5) -194
- 6) -178

## Exercise 2

Compute  $\int_0^1 (e^{2-t} (2 + 3t^2)) dt$

- 1) -62.3109
- 2) 12.9017
- 3) 8.15485
- 4) -59.3403
- 5) -8.15485
- 6) -51.5506

## Exercise 3

Compute  $\int_{-4}^{-1} \left(\frac{5}{t^5}\right) dt$

- 1)  $4.19328 \times 10^6$
- 2) -6.01352
- 3) -1.24512
- 4) -4.96221
- 5) -4.97506
- 6) -5.72683

## Exercise 4

Compute  $\int_5^7 \left( \frac{-3 - 9a - 3t + 3at}{-3 - 2t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter a.  
Compute the derivative of such a formula at the point 0.

- 1) 1.08895
- 2) The rest of the solutions are not correct
- 3) -0.131554
- 4) 0.195146
- 5) 1.00715
- 6) 0.573046

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (9 + 6t)e^{1+3t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 70 millions of euros, compute the deposits available after 1 year.

- 1)  $70 - \frac{7e}{3} + \frac{19e^7}{3}$  millions of euros = 7009.0007 millions of euros
- 2)  $70 + \frac{1}{3e^2} - \frac{7e}{3}$  millions of euros = 63.7025 millions of euros
- 3)  $70 - \frac{7e}{3} + \frac{25e^{10}}{3}$  millions of euros = 183617.539 millions of euros
- 4)  $70 - \frac{7e}{3} + \frac{13e^4}{3}$  millions of euros = 300.2493 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = \cos(-7 + 7t) \text{ euros.}$$

Compute the average value of the shares along the first  $\pi$  months of the year (between  $t=0$  and  $t=\pi$ ).

- 1)  $50 + \frac{2 \text{Sin}[7]}{7\pi}$  euros = 50.0598 euros
- 2)  $-30 + \frac{2 \text{Sin}[7]}{7\pi}$  euros = -29.9402 euros
- 3)  $-70 + \frac{2 \text{Sin}[7]}{7\pi}$  euros = -69.9402 euros
- 4)  $\frac{2 \text{Sin}[7]}{7\pi}$  euros = 0.0598 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 9x + 6x^2 - 3x^3$  and the horizontal axis between the points  $x=1$  and  $x=4$ .

1)  $\frac{9}{4} = 2.25$

2)  $\frac{227}{4} = 56.75$

3)  $\frac{215}{4} = 53.75$

4)  $\frac{221}{4} = 55.25$

5)  $\frac{225}{4} = 56.25$

6)  $\frac{229}{4} = 57.25$

7)  $\frac{223}{4} = 55.75$

8)  $\frac{231}{4} = 57.75$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \cos(5 + 6t) \text{ per-unit.}$$

The initial deposit in the account is 18000 euros. Compute the deposit after  $2\pi$  years.

1) 17910 euros

2) 18000 euros

3) 17920 euros

4) 18080 euros



## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 21055224

#### Exercise 1

Compute  $\int_{-2a}^1 (-1 - 8a - 8t + 4at + 3t^2 + 24at^2 + 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) -9
- 2) 5
- 3) The rest of the solutions are not correct
- 4) -6
- 5) 4
- 6)  $\emptyset$

#### Exercise 2

Compute  $\int_{-6}^5 (\text{Log}[-2t]) dt$

- 1) -10.7764
- 2) -4.75106
- 3) 2.39651
- 4) -20.892
- 5) -11.0002
- 6) -10.4416

#### Exercise 3

Compute  $\int_{-3}^{-2} \left( \frac{486}{(-1-3t)^4} \right) dt$

- 1) -4.5901
- 2) -4.35701
- 3) -1.98249
- 4) 0.326531
- 5) -4.49668
- 6) 9881.

## Exercise 4

Compute  $\int_4^5 \left( \frac{-10 - 6a - 5t + 3at}{-4 + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) 0.712152
- 2) -0.214048
- 3) The rest of the solutions are not correct
- 4) 0.684152
- 5) 0.137152
- 6) 0.462452

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (5 + 3t)e^{-3+2t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 40 millions of euros, compute the deposits available after 2 years.

- 1)  $40 - \frac{7}{4e^3} + \frac{19e}{4}$  millions of euros = 52.8247 millions of euros
- 2)  $40 - \frac{7}{4e^3} + \frac{13}{4e}$  millions of euros = 41.1085 millions of euros
- 3)  $40 + \frac{1}{4e^5} - \frac{7}{4e^3}$  millions of euros = 39.9146 millions of euros
- 4)  $40 - \frac{7}{4e^3} + \frac{25e^3}{4}$  millions of euros = 165.4475 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = 20e^{2+2t} \text{ euros.}$$

Compute the average value of the shares along the first 5 months of the year (between  $t=0$  and  $t=5$ ).

- 1)  $\frac{1}{5} (-10e^2 + 10e^4)$  euros = 94.4182 euros
- 2)  $\frac{1}{5} (10 - 10e^2)$  euros = -12.7781 euros
- 3)  $\frac{1}{5} (-10e^2 + 10e^6)$  euros = 792.0795 euros
- 4)  $\frac{1}{5} (-10e^2 + 10e^{12})$  euros = 325494.8047 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -12 + 3x^2$  and the horizontal axis between the points  $x=-2$  and  $x=4$ .

- 1)  $\frac{131}{2} = 65.5$
- 2) 64
- 3) 67
- 4) 68
- 5) 0
- 6) 66
- 7)  $\frac{133}{2} = 66.5$
- 8)  $\frac{135}{2} = 67.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{13} e^{-4+2t} \text{ per-unit.}$$

The initial deposit in the account is 5000 euros. Compute the deposit after 2 years.

- 1) 5262.3947 euros
- 2) 5192.3947 euros
- 3) 5202.3947 euros
- 4) 5282.3947 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 26052770

## Exercise 1

Compute  $\int_{-2a}^3 (-4 + 20a + 20t - 24at - 18t^2 + 6at^2 + 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) -3
- 2) -16
- 3) The rest of the solutions are not correct
- 4) -6
- 5) -20
- 6) -2

## Exercise 2

Compute  $\int_0^1 (e^{-3+2t} (8 + 12t - 12t^2)) dt$

- 1) -6.10414
- 2) -7.36023
- 3) -4.65171
- 4) -6.30196
- 5) 3.67879
- 6) 1.57109

## Exercise 3

Compute  $\int_{-9}^{-1} \left(\frac{9}{t^4}\right) dt$

- 1) 2.99588
- 2) -11.6399
- 3) -12.0171
- 4) -8.87026
- 5)  $-6.15083 \times 10^7$
- 6) -14.0351

## Exercise 4

Compute  $\int_3^5 \left( \frac{-2+t-4at}{-2t+t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) -4.97765
- 2) -4.70525
- 3) -4.39445
- 4) -4.59045
- 5) -4.63905
- 6) The rest of the solutions are not correct

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (7 + 4t)(\sin(2\pi t) + 2) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 80 millions of euros, compute the deposits available after 4 years.

- 1)  $70 + \frac{2}{\pi}$  millions of euros = 70.6366 millions of euros
- 2)  $98 - \frac{2}{\pi}$  millions of euros = 97.3634 millions of euros
- 3)  $200 - \frac{8}{\pi}$  millions of euros = 197.4535 millions of euros
- 4)  $124 - \frac{4}{\pi}$  millions of euros = 122.7268 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = (3 + 6t)(\sin(2\pi t) + 2) \text{ euros.}$$

Compute the average value of the shares along the first 6 months of the year (between t=0 and t=6).

- 1)  $\frac{1}{6} \left( 36 - \frac{6}{\pi} \right)$  euros = 5.6817 euros
- 2)  $\frac{1}{6} \left( 12 - \frac{3}{\pi} \right)$  euros = 1.8408 euros
- 3)  $\frac{1}{6} \left( 252 - \frac{18}{\pi} \right)$  euros = 41.0451 euros
- 4)  $\frac{1}{2\pi}$  euros = 0.1592 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 2x - x^2$  and the horizontal axis between the points  $x=-4$  and  $x=5$ .

1)  $\frac{349}{6} = 58.1667$

2)  $\frac{179}{3} = 59.6667$

3)  $\frac{361}{6} = 60.1667$

4)  $\frac{176}{3} = 58.6667$

5)  $\frac{170}{3} = 56.6667$

6) 18

7) 54

8)  $\frac{62}{3} = 20.6667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1}{100} (3 + 6t) \right) (\sin(2\pi t) + 2) \text{ per-unit.}$$

The initial deposit in the account is 13000 euros. Compute the deposit after 5 years.

1) 74978.6101 euros

2) 74988.6101 euros

3) 75008.6101 euros

4) 75038.6101 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 26256869

### Exercise 1

Compute  $\int_a^1 (-6 + 9a - 18t - 2at + 3t^2 - 6at^2 + 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) -6
- 2) The rest of the solutions are not correct
- 3) 12
- 4) -8
- 5) 2
- 6) 5

### Exercise 2

Compute  $\int_0^1 ((2 + 2t + 2t^2) \cos[t]) dt$

- 1) -8.34004
- 2) -6.30681
- 3) -12.066
- 4) -9.52203
- 5) 2.92476
- 6) -11.9251

### Exercise 3

Compute  $\int_2^4 \left(\frac{7}{t^4}\right) dt$

- 1) -2.85154
- 2) 0.255208
- 3) -4.12546
- 4) -338603.
- 5) -3.25567
- 6) -4.07731

## Exercise 4

Compute  $\int_4^7 \left( \frac{4 - 4a - 4t + 2at}{2 - 3t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) 1.73089
- 2) 1.17039
- 3) 0.535994
- 4) The rest of the solutions are not correct
- 5) 2.03739
- 6) 1.38629

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function  $v(t) = 20e^{-2+2t}$  millions of euros/year.

If the initial deposit in the investment fund was 90 millions of euros, compute the deposits available after 2 years.

- 1)  $90 - \frac{10}{e^2} + 10e^4$  millions of euros = 634.6281 millions of euros
- 2)  $90 - \frac{10}{e^2} + 10e^2$  millions of euros = 162.5372 millions of euros
- 3)  $100 - \frac{10}{e^2}$  millions of euros = 98.6466 millions of euros
- 4)  $90 + \frac{10}{e^4} - \frac{10}{e^2}$  millions of euros = 88.8298 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (-1 + 4t) \sin(2t) \text{ euros.}$$

Compute the average value of the shares along the first  $3\pi$  months of the year (between  $t=0$  and  $t=3\pi$ ).

- 1)  $-\frac{2}{3}$  euros = -0.6667 euros
- 2)  $\frac{2}{3}$  euros = 0.6667 euros
- 3) -2 euros
- 4)  $-\frac{4}{3}$  euros = -1.3333 euros



## Exercise 7

Compute the area enclosed by the function  $f(x) = -4 + 6x - 2x^2$  and the horizontal axis between the points  $x=1$  and  $x=4$ .

1)  $\frac{73}{6} = 12.1667$

2)  $\frac{41}{3} = 13.6667$

3)  $\frac{38}{3} = 12.6667$

4)  $\frac{44}{3} = 14.6667$

5)  $\frac{35}{3} = 11.6667$

6)  $\frac{67}{6} = 11.1667$

7)  $\frac{29}{3} = 9.6667$

8)  $\frac{85}{6} = 14.1667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{1}{100}(-1 + 4t)\right) \sin(t) \text{ per-unit.}$$

The initial deposit in the account is 10000 euros. Compute the deposit after  $5\pi$  years.

1) 18383.3937 euros

2) 18373.3937 euros

3) 18433.3937 euros

4) 18283.3937 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 26523012

#### Exercise 1

Compute  $\int_{-3a}^3 (6a + 4t - 18at - 9t^2 + 9at^2 + 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 19
- 2) 18
- 3) 34
- 4) The rest of the solutions are not correct
- 5) 32
- 6) 17

#### Exercise 2

Compute  $\int_0^1 ((12t + 12t^2) \cos[3 + 2t]) dt$

- 1) -12.6564
- 2) -4.79462
- 3) -2.68402
- 4) 2.83662
- 5) -12.4448
- 6) -11.3346

#### Exercise 3

Compute  $\int_{-5}^{-3} \left(-\frac{64}{(-1 - 2t)^3}\right) dt$

- 1) -4.22299
- 2) -4.12152
- 3) -4.71547
- 4) -0.442469
- 5) 2968.
- 6) -4.63662

## Exercise 4

Compute  $\int_4^5 \left( \frac{10 - 3a + 5t + at}{-6 - t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1)  $-0.645349$
- 2) The rest of the solutions are not correct
- 3)  $-0.294449$
- 4)  $-0.442249$
- 5)  $0.154151$
- 6)  $0.671151$

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 3 + 3t^2 + 2t^4 \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 50 millions of euros, compute the deposits available after 3 years.

- 1)  $\frac{384}{5}$  millions of euros = 76.8 millions of euros
- 2)  $\frac{916}{5}$  millions of euros = 183.2 millions of euros
- 3)  $\frac{272}{5}$  millions of euros = 54.4 millions of euros
- 4)  $\frac{2678}{5}$  millions of euros = 535.6 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 10e^{1+2t} \text{ euros.}$$

Compute the average value of the shares along the first 8 months of the year (between  $t=0$  and  $t=8$ ).

- 1)  $\frac{1}{8} (-5e + 5e^3)$  euros = 10.8545 euros
- 2)  $\frac{1}{8} \left( \frac{5}{e} - 5e \right)$  euros = -1.469 euros
- 3)  $\frac{1}{8} (-5e + 5e^{17})$  euros =  $1.5097 \times 10^7$  euros
- 4)  $\frac{1}{8} (-5e + 5e^5)$  euros = 91.0593 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -12x - 2x^2 + 2x^3$  and the horizontal axis between the points  $x = -4$  and  $x = 4$ .

1)  $\frac{451}{3} = 150.3333$

2) 64

3)  $\frac{454}{3} = 151.3333$

4)  $\frac{911}{6} = 151.8333$

5)  $\frac{256}{3} = 85.3333$

6)  $\frac{905}{6} = 150.8333$

7)  $\frac{445}{3} = 148.3333$

8)  $\frac{457}{3} = 152.3333$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{e^{-3+t}}{9} \text{ per-unit.}$$

The initial deposit in the account is 20000 euros. Compute the deposit after 3 years.

1) 22247.0827 euros

2) 22227.0827 euros

3) 22297.0827 euros

4) 22267.0827 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 48143225

#### Exercise 1

Compute  $\int_{-3a}^{-3} (9 + 18a + 12t - 48at - 24t^2 - 27at^2 - 12t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -13
- 2)  $\theta$
- 3) -8
- 4) -10
- 5) The rest of the solutions are not correct
- 6) 2

#### Exercise 2

Compute  $\int_{-1}^1 (-3 \cos[1 + 3t]) dt$

- 1) 1.6661
- 2) -2.65229
- 3) -3.94285
- 4) 3.20937
- 5) -3.65062
- 6) -0.152495

#### Exercise 3

Compute  $\int_{-6}^{\theta} \left(-\frac{27}{1-3t}\right) dt$

- 1) -2.94444
- 2) -70.2855
- 3) -104.485
- 4) -26.5
- 5) -96.7413
- 6) -54.7088

## Exercise 4

Compute  $\int_4^5 \left( \frac{6 - 15a - 2t - 5at}{-9 + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) -3.83834
- 2) -3.28184
- 3) -4.01884
- 4) The rest of the solutions are not correct
- 5) -3.46574
- 6) -3.91254

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (4 + t) \log(2t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 40 millions euros, compute the deposit available after (with respect to  $t=1$ ) 2 years.

- 1)  $18 - \frac{9 \operatorname{Log}[2]}{2} + \frac{65 \operatorname{Log}[10]}{2}$  millions of euros = 89.7149 millions of euros
- 2)  $\frac{97}{4} - \frac{9 \operatorname{Log}[2]}{2} + 24 \operatorname{Log}[8]$  millions of euros = 71.0374 millions of euros
- 3)  $100 - \frac{9 \operatorname{Log}[2]}{2} + \frac{33 \operatorname{Log}[6]}{2}$  millions of euros = 126.4449 millions of euros
- 4)  $30 - \frac{9 \operatorname{Log}[2]}{2} + \frac{33 \operatorname{Log}[6]}{2}$  millions of euros = 56.4449 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (2 + 2t) \log(t) \text{ euros.}$$

Compute the average value of shares between month 1 and month 3 (between  $t=1$  and  $t=3$ ).

- 1)  $\frac{1}{2} \left( -\frac{27}{2} + 24 \operatorname{Log}[4] \right)$  euros = 9.8855 euros
- 2)  $\frac{1}{3} \left( -\frac{27}{2} + 24 \operatorname{Log}[4] \right)$  euros = 6.5904 euros
- 3)  $\frac{1}{3} (-20 + 35 \operatorname{Log}[5])$  euros = 12.1101 euros
- 4)  $\frac{1}{2} (-8 + 15 \operatorname{Log}[3])$  euros = 4.2396 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -18 + 18x + 2x^2 - 2x^3$  and the horizontal axis between the points  $x = -3$  and  $x = 0$ .

1)  $\frac{159}{2} = 79.5$

2)  $\frac{169}{2} = 84.5$

3)  $\frac{161}{2} = 80.5$

4)  $\frac{157}{2} = 78.5$

5)  $\frac{163}{2} = 81.5$

6) 81

7)  $\frac{153}{2} = 76.5$

8)  $\frac{165}{2} = 82.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{4+t}{100}\right) \log(2t) \text{ per-unit.}$$

In the year  $t=1$  we deposit in the account 3000 euros. Compute the deposit in the account after (with respect to  $t=1$ ) 4 years.

1) 5002.0801 euros

2) 4932.0801 euros

3) 4952.0801 euros

4) 5022.0801 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 53956072

### Exercise 1

Compute  $\int_a^{\theta} (-3 - 4a + 8t + 10at - 15t^2 - 12at^2 + 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -3
- 2) -16
- 3) -11
- 4) 4
- 5) The rest of the solutions are not correct
- 6) -17

### Exercise 2

Compute  $\int_0^1 ((-4 - 12t + 4t^2) \sin[2 - 2t]) dt$

- 1) 0.
- 2) -24.6823
- 3) -4.33333
- 4) -17.6388
- 5) -5.52055
- 6) -18.5114

### Exercise 3

Compute  $\int_6^9 \left( \frac{2}{(-3+t)^3} \right) dt$

- 1) 0.0833333
- 2) -4.47099
- 3) -607.5
- 4) -2.50414
- 5) -3.35318
- 6) -3.19512



## Exercise 4

Compute  $\int_1^3 \left( \frac{-2a + 5t - at}{2t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) -0.430712
- 2) The rest of the solutions are not correct
- 3) -0.431712
- 4) -1.79201
- 5) -1.09861
- 6) -0.694412

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 3 + 3t^2 + 3t^3 + t^4 \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 80 millions of euros, compute the deposits available after 3 years.

- 1)  $\frac{2764}{5}$  millions of euros = 552.8 millions of euros
- 2)  $\frac{1699}{20}$  millions of euros = 84.95 millions of euros
- 3)  $\frac{4507}{20}$  millions of euros = 225.35 millions of euros
- 4)  $\frac{562}{5}$  millions of euros = 112.4 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = (6 + 8t)e^{-1+t} \text{ euros.}$$

Compute the average value of the shares along the first 3 months of the year (between t=0 and t=3).

- 1)  $\frac{1}{3} \left( \frac{2}{e} + 22e^2 \right)$  euros = 54.4317 euros
- 2)  $\frac{1}{3} \left( \frac{2}{e} + 14e \right)$  euros = 12.9306 euros
- 3)  $\frac{1}{3} \left( 6 + \frac{2}{e} \right)$  euros = 2.2453 euros
- 4)  $\frac{1}{3} \left( -\frac{10}{e^2} + \frac{2}{e} \right)$  euros = -0.2059 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -2x - x^2$  and the horizontal axis between the points  $x=-4$  and  $x=4$ .

- 1) 32
- 2)  $\frac{142}{3} = 47.3333$
- 3)  $\frac{88}{3} = 29.3333$
- 4)  $\frac{281}{6} = 46.8333$
- 5)  $\frac{145}{3} = 48.3333$
- 6)  $\frac{136}{3} = 45.3333$
- 7)  $\frac{128}{3} = 42.6667$
- 8)  $\frac{287}{6} = 47.8333$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{3-t}{20}\right) e^{-1+t} \text{ per-unit.}$$

The initial deposit in the account is 7000 euros. Compute the deposit after 1 year.

- 1) 7555.9419 euros
- 2) 7645.9419 euros
- 3) 7535.9419 euros
- 4) 7605.9419 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 74540350

### Exercise 1

Compute  $\int_a^0 (2a - 4t + 8at - 12t^2 - 6at^2 + 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) -9
- 2) 0
- 3) -17
- 4) -1
- 5) -15
- 6) The rest of the solutions are not correct

### Exercise 2

Compute  $\int_{-3}^0 ((1 + 3t) \sin[2 - t]) dt$

- 1) 7.45782
- 2) -26.5375
- 3) 10.0687
- 4) -32.597
- 5) -2.97845
- 6) -29.5969

### Exercise 3

Compute  $\int_{-1}^1 \left( -\frac{192}{(-3 - 2t)^5} \right) dt$

- 1) 23.9616
- 2) -85.2638
- 3) -95.0934
- 4) -104.732
- 5) -3906.
- 6) -83.0745

## Exercise 4

Compute  $\int_4^5 \left( \frac{-4 - 3a - 4t + at}{-3 - 2t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) 0.182322
- 2) 0.149422
- 3) 0.0216216
- 4) -0.144478
- 5) -0.449678
- 6) The rest of the solutions are not correct

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = t + 2t^3 + 3t^4 \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 70 millions of euros, compute the deposits available after 3 years.

- 1)  $\frac{1304}{5}$  millions of euros = 260.8 millions of euros
- 2)  $\frac{496}{5}$  millions of euros = 99.2 millions of euros
- 3)  $\frac{4102}{5}$  millions of euros = 820.4 millions of euros
- 4)  $\frac{358}{5}$  millions of euros = 71.6 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = \sin(2 + 3t) \text{ euros.}$$

Compute the average value of the shares along the first  $\pi$  months of the year (between  $t=0$  and  $t=\pi$ ).

- 1)  $60 + \frac{2 \cos[2]}{3\pi}$  euros = 59.9117 euros
- 2)  $\frac{2 \cos[2]}{3\pi}$  euros = -0.0883 euros
- 3)  $-70 + \frac{2 \cos[2]}{3\pi}$  euros = -70.0883 euros
- 4)  $10 + \frac{2 \cos[2]}{3\pi}$  euros = 9.9117 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -3 - 2x + x^2$  and the horizontal axis between the points  $x = -5$  and  $x = 1$ .

1)  $\frac{176}{3} = 58.6667$

2)  $\frac{188}{3} = 62.6667$

3)  $\frac{379}{6} = 63.1667$

4) 48

5)  $\frac{182}{3} = 60.6667$

6)  $\frac{373}{6} = 62.1667$

7)  $\frac{185}{3} = 61.6667$

8)  $\frac{367}{6} = 61.1667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \sin(-2 + 3t) \text{ per-unit.}$$

The initial deposit in the account is 7000 euros. Compute the deposit after  $2\pi$  years.

1) 7000 euros

2) 6930 euros

3) 7070 euros

4) 7050 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 75573701

### Exercise 1

Compute  $\int_{-3a}^2 (-10 - 21a - 14t + 42at + 21t^2 + 36at^2 + 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 115
- 2) The rest of the solutions are not correct
- 3) 104
- 4) 102
- 5) 113
- 6) 108

### Exercise 2

Compute  $\int_0^1 (-(-12 - 8t + 8t^2) \sin[2 + 2t]) dt$

- 1) -5.58369
- 2) 4.35762
- 3) -6.13683
- 4) 1.59498
- 5) -5.56012
- 6) -10.0907

### Exercise 3

Compute  $\int_2^3 \left( \frac{1024}{(-2 + 4t)^5} \right) dt$

- 1) -3.50078
- 2) -238336.
- 3) 0.0429827
- 4) -3.486
- 5) -3.84758
- 6) -3.2424

## Exercise 4

Compute  $\int_6^7 \left( \frac{4 - 10a + 2t + 5at}{-4 + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter a.  
Compute the derivative of such a formula at the point 0.

- 1) -0.391785
- 2) 0.120515
- 3) The rest of the solutions are not correct
- 4) 0.588915
- 5) -0.289685
- 6) 0.532615

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (3 + 3t) \log(2t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 90 millions euros, compute the deposit available after (with respect to  $t=1$ ) 5 years.

- 1)  $\frac{235}{4} - \frac{9 \log[2]}{2} + 72 \log[12]$  millions of euros = 234.5441 millions of euros
- 2)  $\frac{279}{4} - \frac{9 \log[2]}{2} + 36 \log[8]$  millions of euros = 141.4907 millions of euros
- 3)  $60 - \frac{9 \log[2]}{2} + \frac{105 \log[10]}{2}$  millions of euros = 177.7666 millions of euros
- 4)  $\frac{195}{4} - \frac{9 \log[2]}{2} + 72 \log[12]$  millions of euros = 224.5441 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 30 e^{2+2t} \text{ euros.}$$

Compute the average value of the shares along the first 7 months of the year (between  $t=0$  and  $t=7$ ).

- 1)  $\frac{1}{7} (-15 e^2 + 15 e^6)$  euros = 848.6566 euros
- 2)  $\frac{1}{7} (15 - 15 e^2)$  euros = -13.6908 euros
- 3)  $\frac{1}{7} (-15 e^2 + 15 e^4)$  euros = 101.1623 euros
- 4)  $\frac{1}{7} (-15 e^2 + 15 e^{16})$  euros =  $1.9042 \times 10^7$  euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 4 - 4x - x^2 + x^3$  and the horizontal axis between the points  $x = -4$  and  $x = 4$ .

1)  $\frac{361}{6} = 60.1667$

2)  $\frac{32}{3} = 10.6667$

3)  $\frac{527}{6} = 87.8333$

4)  $\frac{515}{6} = 85.8333$

5)  $\frac{248}{3} = 82.6667$

6)  $\frac{503}{6} = 83.8333$

7)  $\frac{256}{3} = 85.3333$

8)  $\frac{521}{6} = 86.8333$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{14} e^{-9+3t} \text{ per-unit.}$$

The initial deposit in the account is 14000 euros. Compute the deposit after 3 years.

1) 14377.2911 euros

2) 14337.2911 euros

3) 14427.2911 euros

4) 14327.2911 euros



## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 77379111

#### Exercise 1

Compute  $\int_a^5 (8 - 6a + 12t + 22at - 33t^2 - 9at^2 + 12t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -148
- 2) -122
- 3) -146
- 4) -134
- 5) The rest of the solutions are not correct
- 6) -138

#### Exercise 2

Compute  $\int_0^1 ((9 - 18t^2) \cos[1 + 3t]) dt$

- 1) -3.83295
- 2) -0.756802
- 3) -4.32276
- 4) -1.96093
- 5) 0.229538
- 6) -3.79259

#### Exercise 3

Compute  $\int_{-6}^{-3} \left(\frac{9}{t^3}\right) dt$

- 1) 607.5
- 2) -4.32276
- 3) -3.79259
- 4) -0.375
- 5) -2.62945
- 6) -3.83295

## Exercise 4

Compute  $\int_2^3 \left( \frac{-6a - 3t - 2at}{3t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1)  $-0.46013$
- 2) The rest of the solutions are not correct
- 3)  $-1.33463$
- 4)  $-1.09853$
- 5)  $-0.81093$
- 6)  $-1.41043$

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function  $v(t) = 20e^{-2+t}$  millions of euros/year.

If the initial deposit in the investment fund was  $80$  millions of euros, compute the deposits available after  $2$  years.

- 1)  $80 + \frac{20}{e^3} - \frac{20}{e^2}$  millions of euros =  $78.289$  millions of euros
- 2)  $80 - \frac{20}{e^2} + 20e$  millions of euros =  $131.6589$  millions of euros
- 3)  $80 - \frac{20}{e^2} + \frac{20}{e}$  millions of euros =  $84.6509$  millions of euros
- 4)  $100 - \frac{20}{e^2}$  millions of euros =  $97.2933$  millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (5 + 2t)e^{2t} \text{ euros.}$$

Compute the average value of the shares along the first  $4$  months of the year (between  $t=0$  and  $t=4$ ).

- 1)  $\frac{1}{4} (-2 + 4e^4)$  euros =  $54.0982$  euros
- 2)  $\frac{1}{4} (-2 + 6e^8)$  euros =  $4470.937$  euros
- 3)  $\frac{1}{4} (-2 + 3e^2)$  euros =  $5.0418$  euros
- 4)  $\frac{1}{4} \left( -2 + \frac{1}{e^2} \right)$  euros =  $-0.4662$  euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -6x - 2x^2$  and the horizontal axis between the points  $x = -5$  and  $x = -2$ .

1)  $\frac{127}{6} = 21.1667$

2) 15

3)  $\frac{139}{6} = 23.1667$

4)  $\frac{65}{3} = 21.6667$

5)  $\frac{71}{3} = 23.6667$

6)  $\frac{68}{3} = 22.6667$

7)  $\frac{145}{6} = 24.1667$

8)  $\frac{59}{3} = 19.6667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{3+t}{13}\right) e^{-3+t} \text{ per-unit.}$$

The initial deposit in the account is 1000 euros. Compute the deposit after 1 year.

1) 1083.8517 euros

2) 1113.8517 euros

3) 1023.8517 euros

4) 1033.8517 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 77388334

### Exercise 1

Compute  $\int_{2a}^1 (9 - 24a + 24t + 8at - 6t^2 + 6at^2 - 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -36
- 2) -52
- 3) -43
- 4) The rest of the solutions are not correct
- 5) -39
- 6) -45

### Exercise 2

Compute  $\int_3^5 ((-8 - 12t - 4t^2) \text{Log}[2t]) dt$

- 1) -616.995
- 2) -509.439
- 3) -2052.16
- 4) -1306.06
- 5) -1416.63
- 6) -1735.75

### Exercise 3

Compute  $\int_4^9 \left( \frac{4}{(1-2t)^2} \right) dt$

- 1) -2.56371
- 2) 4570.
- 3) 0.168067
- 4) -3.40717
- 5) -2.45326
- 6) -2.78075

## Exercise 4

Compute  $\int_2^3 \left( \frac{-2 + 3a - 2t - 3at}{-1 + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2)  $-1.00125$
- 3)  $-0.863046$
- 4)  $-1.02775$
- 5)  $-0.271346$
- 6)  $-0.709046$

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (3 + 6t)e^{3+t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was  $70$  millions of euros, compute the deposits available after  $2$  years.

- 1)  $70 + 3e^3 + 15e^6$  millions of euros =  $6181.6885$  millions of euros
- 2)  $70 - 9e^2 + 3e^3$  millions of euros =  $63.7551$  millions of euros
- 3)  $70 + 3e^3 + 3e^4$  millions of euros =  $294.0511$  millions of euros
- 4)  $70 + 3e^3 + 9e^5$  millions of euros =  $1465.975$  millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = \sin(-5 + 7t) \text{ euros.}$$

Compute the average value of the shares along the first  $2\pi$  months of the year (between  $t=0$  and  $t=2\pi$ ).

- 1)  $20$  euros
- 2)  $-40$  euros
- 3)  $30$  euros
- 4)  $0$  euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 3 - 3x^2$  and the horizontal axis between the points  $x = -3$  and  $x = 1$ .

- 1) 28
- 2)  $\frac{53}{2} = 26.5$
- 3) 16
- 4)  $\frac{51}{2} = 25.5$
- 5)  $\frac{55}{2} = 27.5$
- 6) 24
- 7)  $\frac{57}{2} = 28.5$
- 8) 27

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \sin(3 + t) \text{ per-unit.}$$

The initial deposit in the account is 20000 euros. Compute the deposit after  $2\pi$  years.

- 1) 19970 euros
- 2) 19980 euros
- 3) 20010 euros
- 4) 20000 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 77434209

### Exercise 1

Compute  $\int_a^3 (-3 - 5a + 10t + 6at - 9t^2 - 3at^2 + 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 63
- 2) 81
- 3) 57
- 4) 87
- 5) 68
- 6) The rest of the solutions are not correct

### Exercise 2

Compute  $\int_2^3 ((-1 + 3t) \text{Log}[t]) dt$

- 1) 8.76284
- 2) -24.6493
- 3) -25.3338
- 4) -21.3722
- 5) 6.01284
- 6) -24.5644

### Exercise 3

Compute  $\int_{-6}^5 \left( \frac{8}{(3 + 2t)^3} \right) dt$

- 1) -4.08532
- 2) -0.016125
- 3) -4.21328
- 4) -4.09945
- 5) 2080.
- 6) -3.55443

## Exercise 4

Compute  $\int_2^3 \left( \frac{-a + 2t + at}{-t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) 0.757765
- 3) 0.405465
- 4) -0.479535
- 5) 0.119565
- 6) -0.0648349

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 2t + 3t^2 + 3t^3 \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 90 millions of euros, compute the deposits available after 3 years.

- 1)  $\frac{371}{4}$  millions of euros = 92.75 millions of euros
- 2) 362 millions of euros
- 3) 114 millions of euros
- 4)  $\frac{747}{4}$  millions of euros = 186.75 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (6 + 6t)e^{-1+2t} \text{ euros.}$$

Compute the average value of the shares along the first 9 months of the year (between  $t=0$  and  $t=9$ ).

- 1)  $\frac{1}{9} \left( -\frac{3}{2e} + \frac{57e^{17}}{2} \right)$  euros =  $7.6491 \times 10^7$  euros
- 2)  $\frac{1}{9} \left( -\frac{3}{2e^3} - \frac{3}{2e} \right)$  euros = -0.0696 euros
- 3)  $\frac{1}{9} \left( -\frac{3}{2e} + \frac{9e}{2} \right)$  euros = 1.2978 euros
- 4)  $\frac{1}{9} \left( -\frac{3}{2e} + \frac{15e^3}{2} \right)$  euros = 16.6766 euros



## Exercise 7

Compute the area enclosed by the function  $f(x) = -6x + 3x^2 + 3x^3$  and the horizontal axis between the points  $x = -2$  and  $x = 3$ .

- 1)  $\frac{303}{4} = 75.75$
- 2)  $\frac{295}{4} = 73.75$
- 3)  $\frac{297}{4} = 74.25$
- 4)  $\frac{275}{4} = 68.75$
- 5)  $\frac{301}{4} = 75.25$
- 6)  $\frac{285}{4} = 71.25$
- 7)  $\frac{211}{4} = 52.75$
- 8)  $\frac{293}{4} = 73.25$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1}{18} (-2 + 3t) \right) e^{-2+3t} \text{ per-unit.}$$

The initial deposit in the account is 18000 euros. Compute the deposit after 1 year.

- 1) 18225.8453 euros
- 2) 18155.8453 euros
- 3) 18135.8453 euros
- 4) 18215.8453 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 77435467

### Exercise 1

Compute  $\int_{-2a}^1 (-4 + 10a + 10t - 8at - 6t^2 + 6at^2 + 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2)  $0$
- 3)  $-9$
- 4)  $3$
- 5)  $-20$
- 6)  $5$

### Exercise 2

Compute  $\int_{-6}^1 ((-6 - 3t) \text{Log}[-3t]) dt$

- 1)  $-279.112$
- 2)  $-255.575$
- 3)  $60.7204$
- 4)  $-214.559$
- 5)  $-204.604$
- 6)  $56.9704$

### Exercise 3

Compute  $\int_{-9}^1 \left(-\frac{5120}{(5-4t)^5}\right) dt$

- 1)  $-1346.89$
- 2)  $-320.$
- 3)  $-1470.94$
- 4)  $1.18753 \times 10^9$
- 5)  $-1130.74$
- 6)  $-1094.66$

## Exercise 4

Compute  $\int_3^5 \left( \frac{6 - 4a + 2t + 2at}{-6 + t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1)  $-0.112636$
- 2) The rest of the solutions are not correct
- 3)  $0.455964$
- 4)  $0.575364$
- 5)  $0.848664$
- 6)  $0.169364$

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function  $v(t) = 30e^{2t}$  millions of euros/year.

If the initial deposit in the investment fund was 30 millions of euros, compute the deposits available after 1 year.

- 1)  $15 + 15e^6$  millions of euros = 6066.4319 millions of euros
- 2)  $15 + 15e^4$  millions of euros = 833.9723 millions of euros
- 3)  $15 + \frac{15}{e^2}$  millions of euros = 17.03 millions of euros
- 4)  $15 + 15e^2$  millions of euros = 125.8358 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 3t + 3t^4 \text{ euros.}$$

Compute the average value of the shares along the first 9 months of the year (between  $t=0$  and  $t=9$ ).

- 1)  $\frac{177}{10}$  euros = 17.7 euros
- 2)  $\frac{7}{30}$  euros = 0.2333 euros
- 3)  $\frac{14}{5}$  euros = 2.8 euros
- 4)  $\frac{39501}{10}$  euros = 3950.1 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -18x + 3x^2 + 3x^3$  and the horizontal axis between the points  $x = -5$  and  $x = 2$ .

$$1) \frac{411}{4} = 102.75$$

$$2) \frac{789}{4} = 197.25$$

$$3) \frac{925}{4} = 231.25$$

$$4) \frac{917}{4} = 229.25$$

$$5) \frac{923}{4} = 230.75$$

$$6) \frac{539}{4} = 134.75$$

$$7) \frac{927}{4} = 231.75$$

$$8) \frac{929}{4} = 232.25$$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{100} (t + t^3 + 2t^4) \text{ per-unit.}$$

The initial deposit in the account is 16000 euros. Compute the deposit after 2 years.

$$1) 19329.3362 \text{ euros}$$

$$2) 19289.3362 \text{ euros}$$

$$3) 19319.3362 \text{ euros}$$

$$4) 19309.3362 \text{ euros}$$

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 77647383

#### Exercise 1

Compute  $\int_{3a}^5 (-12 - 15a + 10t + 36at - 18t^2 + 27at^2 - 12t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 1533
- 2) 1551
- 3) 1536
- 4) The rest of the solutions are not correct
- 5) 1548
- 6) 1542

#### Exercise 2

Compute  $\int_{-1}^0 (-3 \cos[1 + 2t]) dt$

- 1) -2.52441
- 2) 1.26221
- 3) -9.44564
- 4) -10.7924
- 5) -10.0694
- 6) -10.5683

#### Exercise 3

Compute  $\int_4^6 \left(\frac{1}{t}\right) dt$

 **N:** Internal precision limit \$MaxExtraPrecision = 50.` reached while evaluating  $-\text{Log}\left[\frac{3}{2}\right] - \text{Log}[4] + \text{Log}[6]$ .

- 1) 0.405465
- 2) -3.98881
- 3) -3.74172
- 4) -4.27521
- 5) -3.5919
- 6) -4.18643

## Exercise 4

Compute  $\int_1^2 \left( \frac{6a - t + 3at}{2t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\emptyset$ .

- 1) The rest of the solutions are not correct
- 2) 1.54634
- 3) 2.01234
- 4) 2.07944
- 5) 1.83514
- 6) 1.46244

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (1 + 2t)e^t \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 80 millions of euros, compute the deposits available after 1 year.

- 1)  $81 - \frac{3}{e}$  millions of euros = 79.8964 millions of euros
- 2)  $81 + 3e^2$  millions of euros = 103.1672 millions of euros
- 3)  $81 + e$  millions of euros = 83.7183 millions of euros
- 4)  $81 + 5e^3$  millions of euros = 181.4277 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (1 + 2t)e^{1+2t} \text{ euros.}$$

Compute the average value of the shares along the first 8 months of the year (between  $t=0$  and  $t=8$ ).

- 1)  $-\frac{1}{8e}$  euros = -0.046 euros
- 2)  $\frac{e^3}{8}$  euros = 2.5107 euros
- 3)  $e^{17}$  euros =  $2.4155 \times 10^7$  euros
- 4)  $\frac{e^5}{4}$  euros = 37.1033 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 12x + 10x^2 + 2x^3$  and the horizontal axis between the points  $x = -3$  and  $x = 4$ .

1)  $\frac{2587}{6} = 431.1667$

2) 447

3) 445

4)  $\frac{895}{2} = 447.5$

5)  $\frac{2597}{6} = 432.8333$

6)  $\frac{891}{2} = 445.5$

7)  $\frac{893}{2} = 446.5$

8)  $\frac{887}{2} = 443.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1-t}{210678} \right) e^{3t} \text{ per-unit.}$$

The initial deposit in the account is 13000 euros. Compute the deposit after 3 years.

1) 12765.1392 euros

2) 12745.1392 euros

3) 12815.1392 euros

4) 12725.1392 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 77648906

## Exercise 1

Compute  $\int_{2a}^{-5} (-4 + 36at - 27t^2 + 30at^2 - 20t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -790
- 2) -808
- 3) -792
- 4) -801
- 5) The rest of the solutions are not correct
- 6) -797

## Exercise 2

Compute  $\int_2^6 (-3 \text{Log}[3t]) dt$

- 1) -135.682
- 2) -29.2761
- 3) -194.659
- 4) -95.6192
- 5) -41.2761
- 6) -108.239

## Exercise 3

Compute  $\int_{-8}^6 \left(-\frac{15}{5-5t}\right) dt$

- 1) -3.69719
- 2) -3.26611
- 3) -3.2605
- 4) -4.63456
- 5) -0.753943
- 6) -0.251314



## Exercise 4

Compute  $\int_5^6 \left( \frac{-3 + 5a + t - 5at}{3 - 4t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) -2.76243
- 2) -2.06643
- 3) -2.55033
- 4) The rest of the solutions are not correct
- 5) -1.76893
- 6) -2.70683

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (2 + t) \log(2t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 20 millions euros, compute the deposit available after (with respect to  $t=1$ ) 2 years.

- 1)  $6 - \frac{5 \operatorname{Log}[2]}{2} + \frac{45 \operatorname{Log}[10]}{2}$  millions of euros = 56.0753 millions of euros
- 2)  $14 - \frac{5 \operatorname{Log}[2]}{2} + \frac{21 \operatorname{Log}[6]}{2}$  millions of euros = 31.0806 millions of euros
- 3)  $-6 - \frac{5 \operatorname{Log}[2]}{2} + \frac{21 \operatorname{Log}[6]}{2}$  millions of euros = 11.0806 millions of euros
- 4)  $\frac{41}{4} - \frac{5 \operatorname{Log}[2]}{2} + 16 \operatorname{Log}[8]$  millions of euros = 41.7882 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (2 + t) \log(2t) \text{ euros.}$$

Compute the average value of shares between month 1 and month 3 (between  $t=1$  and  $t=3$ ).

- 1)  $\frac{1}{2} \left( -6 - \frac{5 \operatorname{Log}[2]}{2} + \frac{21 \operatorname{Log}[6]}{2} \right)$  euros = 5.5403 euros
- 2)  $\frac{1}{2} \left( -\frac{39}{4} - \frac{5 \operatorname{Log}[2]}{2} + 16 \operatorname{Log}[8] \right)$  euros = 10.8941 euros
- 3)  $\frac{1}{3} \left( -14 - \frac{5 \operatorname{Log}[2]}{2} + \frac{45 \operatorname{Log}[10]}{2} \right)$  euros = 12.0251 euros
- 4)  $\frac{1}{3} \left( -\frac{39}{4} - \frac{5 \operatorname{Log}[2]}{2} + 16 \operatorname{Log}[8] \right)$  euros = 7.2627 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -18 + 15x + 6x^2 - 3x^3$  and the horizontal axis between the points  $x = -3$  and  $x = 5$ .

- 1)  $\frac{451}{2} = 225.5$
- 2) 224
- 3)  $\frac{445}{2} = 222.5$
- 4) 128
- 5) 225
- 6) 96
- 7)  $\frac{381}{2} = 190.5$
- 8)  $\frac{449}{2} = 224.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{2+t}{100}\right) \log(2t) \text{ per-unit.}$$

In the year  $t=1$  we deposit in the account 17000 euros. Compute the deposit in the account after (with respect to  $t=1$ ) 5 years.

- 1) 29280.8896 euros
- 2) 29170.8896 euros
- 3) 29190.8896 euros
- 4) 29200.8896 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 77770524

### Exercise 1

Compute  $\int_{-a}^3 (-6 - 5a - 10t - 26at - 39t^2 - 12at^2 - 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) -263
- 3) -246
- 4) -251
- 5) -252
- 6) -259

### Exercise 2

Compute  $\int_{-5}^4 ((-4 - 12t - 4t^2) \text{Log}[-2t]) dt$

- 1) -313.464
- 2) 215.779
- 3) -73.3378
- 4) -308.081
- 5) -290.667
- 6) -69.2267

### Exercise 3

Compute  $\int_{-6}^3 \left(-\frac{9216}{(4-4t)^5}\right) dt$

- 1) -3.12174
- 2) -0.00785195
- 3)  $1.16278 \times 10^8$
- 4) -4.45032
- 5) -4.19878
- 6) -4.52808

## Exercise 4

Compute  $\int_3^4 \left( \frac{6 + 8a + 2t - 4at}{-6 + t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1)  $-0.443003$
- 2)  $-1.4896$
- 3)  $-1.6137$
- 4)  $-0.930203$
- 5)  $-1.2165$
- 6) The rest of the solutions are not correct

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (7 + 3t)(\sin(2\pi t) + 1) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 30 millions of euros, compute the deposits available after 4 years.

- 1)  $50 - \frac{3}{\pi}$  millions of euros = 49.0451 millions of euros
- 2)  $82 - \frac{6}{\pi}$  millions of euros = 80.0901 millions of euros
- 3)  $\frac{77}{2} - \frac{3}{2\pi}$  millions of euros = 38.0225 millions of euros
- 4)  $\frac{49}{2} + \frac{3}{2\pi}$  millions of euros = 24.9775 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 3 + 3t + 2t^2 + t^3 + 2t^4 \text{ euros.}$$

Compute the average value of the shares along the first 9 months of the year (between  $t=0$  and  $t=9$ ).

- 1)  $\frac{512}{135}$  euros = 3.7926 euros
- 2)  $\frac{57543}{20}$  euros = 2877.15 euros
- 3)  $\frac{351}{20}$  euros = 17.55 euros
- 4)  $\frac{349}{540}$  euros = 0.6463 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -18 + 21x - 3x^3$  and the horizontal axis between the points  $x = -1$  and  $x = 2$ .

1)  $\frac{159}{4} = 39.75$

2)  $\frac{165}{4} = 41.25$

3)  $\frac{153}{4} = 38.25$

4)  $\frac{167}{4} = 41.75$

5)  $\frac{135}{4} = 33.75$

6)  $\frac{163}{4} = 40.75$

7)  $\frac{161}{4} = 40.25$

8)  $\frac{171}{4} = 42.75$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{3+t}{100} \text{ per-unit.}$$

The initial deposit in the account is 10000 euros. Compute the deposit after 1 year.

1) 10346.1971 euros

2) 10356.1971 euros

3) 10336.1971 euros

4) 10386.1971 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

### List of exercises 03-Integration for identity number: 78026316

#### Exercise 1

Compute  $\int_a^4 (6 - 7a + 14t - 20at + 30t^2 - 12at^2 + 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) -463
- 3) -452
- 4) -459
- 5) -468
- 6) -469

#### Exercise 2

Compute  $\int_0^1 ((12t + 12t^2) \cos[3 - 2t]) dt$

- 1) -0.163901
- 2) -4.24793
- 3) -3.46717
- 4) -3.55495
- 5) 5.40302
- 6) -4.20735

#### Exercise 3

Compute  $\int_5^7 \left( \frac{8}{(2+t)^3} \right) dt$

- 1) -3.46717
- 2) -4.24793
- 3) -3.15188
- 4) 0.0322499
- 5) -3.55495
- 6) -2080.

## Exercise 4

Compute  $\int_2^5 \left( \frac{4a - 5t + 2at}{2t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) 1.08568
- 2) The rest of the solutions are not correct
- 3) 1.15808
- 4) 0.991781
- 5) 1.38218
- 6) 1.83258

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 10e^{3+2t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 80 millions of euros, compute the deposits available after 2 years.

- 1)  $80 - 5e^3 + 5e^7$  millions of euros = 5462.7381 millions of euros
- 2)  $80 - 5e^3 + 5e^5$  millions of euros = 721.6381 millions of euros
- 3)  $80 + 5e - 5e^3$  millions of euros = -6.8363 millions of euros
- 4)  $80 - 5e^3 + 5e^9$  millions of euros = 40494.992 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = (8 + 5t)e^{1+3t} \text{ euros.}$$

Compute the average value of the shares along the first 4 months of the year (between t=0 and t=4).

- 1)  $\frac{1}{4} \left( -\frac{19e}{9} + \frac{34e^4}{9} \right)$  euros = 50.1303 euros
- 2)  $\frac{1}{4} \left( \frac{4}{9e^2} - \frac{19e}{9} \right)$  euros = -1.4196 euros
- 3)  $\frac{1}{4} \left( -\frac{19e}{9} + \frac{49e^7}{9} \right)$  euros = 1491.2049 euros
- 4)  $\frac{1}{4} \left( -\frac{19e}{9} + \frac{79e^{13}}{9} \right)$  euros = 970850.1756 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -4x - 2x^2$  and the horizontal axis between the points  $x=-3$  and  $x=2$ .

1)  $\frac{121}{6} = 20.1667$

2)  $\frac{133}{6} = 22.1667$

3)  $\frac{56}{3} = 18.6667$

4)  $\frac{71}{3} = 23.6667$

5)  $\frac{62}{3} = 20.6667$

6)  $\frac{65}{3} = 21.6667$

7)  $\frac{40}{3} = 13.3333$

8) 8

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1-3t}{1635} \right) e^{2+2t} \text{ per-unit.}$$

The initial deposit in the account is 8000 euros. Compute the deposit after 1 year.

1) 7888.8003 euros

2) 7958.8003 euros

3) 7948.8003 euros

4) 7908.8003 euros



## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 78428692

### Exercise 1

Compute  $\int_{3a}^{-1} (-4 + 27a - 18t - 45at^2 + 20t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) 1
- 2) -19
- 3) 8
- 4) The rest of the solutions are not correct
- 5) -8
- 6) 5

### Exercise 2

Compute  $\int_{-2}^2 ((-6 + 4t) \sin[1 + 2t]) dt$

- 1) -16.5968
- 2) -15.4771
- 3) -9.3326
- 4) -19.7895
- 5) -25.2302
- 6) 5.82848

### Exercise 3

Compute  $\int_6^7 \left( \frac{1}{(-3 + t)^2} \right) dt$

- 1) -3.39531
- 2) 0.0833333
- 3) -37.
- 4) -4.32878
- 5) -2.84754
- 6) -2.65543

## Exercise 4

Compute  $\int_4^5 \left( \frac{-10 + 10a + 5t + 5at}{-4 + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) 1.54483
- 2) 1.76283
- 3) 1.49623
- 4) 2.02733
- 5) 2.30333
- 6) The rest of the solutions are not correct

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (2 + 4t) \log(5t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 80 millions euros, compute the deposit available after (with respect to  $t=1$ ) 4 years.

- 1)  $88 - 4 \log[5] + 60 \log[25]$  millions of euros = 274.6948 millions of euros
- 2)  $59 - 4 \log[5] + 40 \log[20]$  millions of euros = 172.3915 millions of euros
- 3)  $35 - 4 \log[5] + 84 \log[30]$  millions of euros = 314.2628 millions of euros
- 4)  $48 - 4 \log[5] + 60 \log[25]$  millions of euros = 234.6948 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (2 + 8t) (\cos(2\pi t) + 2) \text{ euros.}$$

Compute the average value of the shares along the first 6 months of the year (between  $t=0$  and  $t=6$ ).

- 1)  $\frac{20}{3}$  euros = 6.6667 euros
- 2)  $\frac{2}{3}$  euros = 0.6667 euros
- 3) 52 euros
- 4) 2 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 4 - 4x - x^2 + x^3$  and the horizontal axis between the points  $x = -2$  and  $x = 5$ .

1)  $\frac{1165}{12} = 97.0833$

2)  $\frac{1159}{12} = 96.5833$

3)  $\frac{1189}{12} = 99.0833$

4)  $\frac{1127}{12} = 93.9167$

5)  $\frac{1177}{12} = 98.0833$

6)  $\frac{1141}{12} = 95.0833$

7)  $\frac{1171}{12} = 97.5833$

8)  $\frac{857}{12} = 71.4167$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1}{100} (4 + 5t) \right) (\cos(2\pi t) + 2) \text{ per-unit.}$$

The initial deposit in the account is 20000 euros. Compute the deposit after 3 years.

1) 39874.3107 euros

2) 39934.3107 euros

3) 39944.3107 euros

4) 39954.3107 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number: 753486173

## Exercise 1

Compute  $\int_{3a}^5 (-1 + 3a - 2t - 12at + 6t^2 - 18at^2 + 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -878
- 2) -892
- 3) -902
- 4) -882
- 5) The rest of the solutions are not correct
- 6) -901

## Exercise 2

Compute  $\int_0^2 (6t \cos[1 + 2t]) dt$

- 1) -30.17
- 2) -6.13851
- 3) -19.7114
- 4) 3.40395
- 5) -30.5626
- 6) -24.1583

## Exercise 3

Compute  $\int_{-4}^{-1} \left(\frac{8}{t^2}\right) dt$

- 1) -29.873
- 2) -19.2667
- 3) 6.
- 4) -23.6132
- 5) -504.
- 6) -29.4893

## Exercise 4

Compute  $\int_4^7 \left( \frac{6 - 9a + 3t + 3at}{-6 - t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) 0.350995
- 3) 1.2164
- 4) 0.671095
- 5) 1.1099
- 6) 0.688595

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (2 + 2t)e^t \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 90 millions of euros, compute the deposits available after 2 years.

- 1)  $90 - \frac{2}{e}$  millions of euros = 89.2642 millions of euros
- 2)  $90 + 6e^3$  millions of euros = 210.5132 millions of euros
- 3)  $90 + 4e^2$  millions of euros = 119.5562 millions of euros
- 4)  $90 + 2e$  millions of euros = 95.4366 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 20e^{3+3t} \text{ euros.}$$

Compute the average value of the shares along the first 8 months of the year (between  $t=0$  and  $t=8$ ).

- 1)  $\frac{1}{8} \left( -\frac{20e^3}{3} + \frac{20e^{27}}{3} \right)$  euros =  $4.4337 \times 10^{11}$  euros
- 2)  $\frac{1}{8} \left( -\frac{20e^3}{3} + \frac{20e^9}{3} \right)$  euros = 6735.832 euros
- 3)  $\frac{1}{8} \left( \frac{20}{3} - \frac{20e^3}{3} \right)$  euros = -15.9046 euros
- 4)  $\frac{1}{8} \left( -\frac{20e^3}{3} + \frac{20e^6}{3} \right)$  euros = 319.4527 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 12x + 2x^2 - 2x^3$  and the horizontal axis between the points  $x = -3$  and  $x = 4$ .

- 1)  $\frac{245}{3} = 81.6667$
- 2)  $\frac{481}{6} = 80.1667$
- 3)  $\frac{37}{6} = 6.1667$
- 4)  $\frac{242}{3} = 80.6667$
- 5)  $\frac{469}{6} = 78.1667$
- 6)  $\frac{91}{6} = 15.1667$
- 7)  $\frac{487}{6} = 81.1667$
- 8)  $\frac{239}{3} = 79.6667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{12} e^{-6+2t} \text{ per-unit.}$$

The initial deposit in the account is 20000 euros. Compute the deposit after 3 years.

- 1) 20848.7847 euros
- 2) 20858.7847 euros
- 3) 20838.7847 euros
- 4) 20850.019 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
10618500094

### Exercise 1

Compute  $\int_{-2a}^3 (6a + 6t - 8at - 6t^2 - 6at^2 - 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1)  $-9\theta$
- 2) The rest of the solutions are not correct
- 3)  $-88$
- 4)  $-74$
- 5)  $-72$
- 6)  $-68$

### Exercise 2

Compute  $\int_{-4}^{-1} ((18t - 9t^2) \text{Log}[-3t]) dt$

- 1)  $-691.245$
- 2)  $-3302.33$
- 3)  $-2157.35$
- 4)  $-821.745$
- 5)  $1994.53$
- 6)  $-1725.8$

### Exercise 3

Compute  $\int_{-1}^9 \left( \frac{243}{(4 + 3t)^5} \right) dt$

- 1)  $-50.5572$
- 2)  $-63.1994$
- 3)  $-2.21876 \times 10^8$
- 4)  $20.25$
- 5)  $-48.917$
- 6)  $-96.7414$

## Exercise 4

Compute  $\int_3^4 \left( \frac{5 + 8a - 5t + 4at}{-2 + t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) 0.86576
- 3) 0.75666
- 4) 1.62186
- 5) 0.98066
- 6) 1.67786

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (9 + 5t)(\cos(2\pi t) + 1) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 70 millions of euros, compute the deposits available after 3 years.

- 1) 98 millions of euros
- 2)  $\frac{163}{2}$  millions of euros = 81.5 millions of euros
- 3)  $\frac{127}{2}$  millions of euros = 63.5 millions of euros
- 4)  $\frac{239}{2}$  millions of euros = 119.5 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (2 - 4t)\cos(3t) \text{ euros.}$$

Compute the average value of the shares along the first  $3\pi$  months of the year (between  $t=0$  and  $t=3\pi$ ).

- 1)  $70 + \frac{8}{27\pi}$  euros = 70.0943 euros
- 2) 0 euros
- 3)  $10 + \frac{8}{27\pi}$  euros = 10.0943 euros
- 4)  $\frac{8}{27\pi}$  euros = 0.0943 euros



## Exercise 7

Compute the area enclosed by the function  $f(x) = -6x + 3x^2 + 3x^3$  and the horizontal axis between the points  $x = -1$  and  $x = 2$ .

1)  $\frac{45}{4} = 11.25$

2)  $\frac{65}{4} = 16.25$

3)  $\frac{69}{4} = 17.25$

4)  $\frac{63}{4} = 15.75$

5)  $\frac{55}{4} = 13.75$

6)  $\frac{19}{4} = 4.75$

7)  $\frac{71}{4} = 17.75$

8)  $\frac{67}{4} = 16.75$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{1}{100}(-5 + 3t)\right) \cos(2t) \text{ per-unit.}$$

The initial deposit in the account is 6000 euros. Compute the deposit after  $3\pi$  years.

1) 6000 euros

2) 6010 euros

3) 6050 euros

4) 6040 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
10901600079

### Exercise 1

Compute  $\int_{2a}^5 (-10a + 10t + 30at^2 - 20t^3) dt$

. The resulting expression is a formula in terms of parameter  
a. Compute the derivative of such a formula at the point 0.

- 1) 1186
- 2) 1180
- 3) 1192
- 4) 1197
- 5) 1190
- 6) The rest of the solutions are not correct

### Exercise 2

Compute  $\int_0^1 (e^{-1+t} (-2 - t + t^2)) dt$

- 1) -1.36788
- 2) -3.39838
- 3) -3.34061
- 4) -2.53885
- 5) -4.17169
- 6) -4.4322

### Exercise 3

Compute  $\int_{-3}^{-1} \left( \frac{576}{(-1 + 4t)^3} \right) dt$

- 1) -7.48397
- 2) -7.95134
- 3) -5.99303
- 4) 13968.
- 5) -2.45396
- 6) -6.09666

## Exercise 4

Compute  $\int_2^4 \left( \frac{-3 + 12a + 3t + 4at}{-3 + 2t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) 3.95645
- 2) The rest of the solutions are not correct
- 3) 4.99395
- 4) 3.81345
- 5) 4.39445
- 6) 3.79075

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (6 + 6t)(\sin(2\pi t) + 2) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 20 millions of euros, compute the deposits available after 4 years.

- 1)  $38 - \frac{3}{\pi}$  millions of euros = 37.0451 millions of euros
- 2)  $68 - \frac{6}{\pi}$  millions of euros = 66.0901 millions of euros
- 3)  $164 - \frac{12}{\pi}$  millions of euros = 160.1803 millions of euros
- 4)  $14 + \frac{3}{\pi}$  millions of euros = 14.9549 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = (3 - 4t)\sin(6t) \text{ euros.}$$

Compute the average value of the shares along the first  $2\pi$  months of the year (between  $t=0$  and  $t=2\pi$ ).

- 1)  $-\frac{1}{3}$  euros = -0.3333 euros
- 2) 1 euros
- 3)  $\frac{1}{3}$  euros = 0.3333 euros
- 4)  $\frac{2}{3}$  euros = 0.6667 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -6 + 4x + 2x^2$  and the horizontal axis between the points  $x=1$  and  $x=5$ .

1)  $\frac{667}{6} = 111.1667$

2)  $\frac{329}{3} = 109.6667$

3)  $\frac{338}{3} = 112.6667$

4)  $\frac{335}{3} = 111.6667$

5)  $\frac{320}{3} = 106.6667$

6)  $\frac{649}{6} = 108.1667$

7)  $\frac{332}{3} = 110.6667$

8)  $\frac{326}{3} = 108.6667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{1}{100} (3 - 4t)\right) \sin(6t) \text{ per-unit.}$$

The initial deposit in the account is 17000 euros. Compute the deposit after  $4\pi$  years.

1) 18415.5463 euros

2) 18455.5463 euros

3) 18485.5463 euros

4) 18495.5463 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:

11116551121

### Exercise 1

Compute  $\int_a^1 (12 + 11a - 22t + 16at - 24t^2 + 3at^2 - 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) -16
- 2) -20
- 3) -35
- 4) -36
- 5) -22
- 6) The rest of the solutions are not correct

### Exercise 2

Compute  $\int_0^1 ((-2 - 2t + t^2) \sin[1 - t]) dt$

- 1) -1.15585
- 2) -4.64673
- 3) 0.
- 4) -2.66667
- 5) -4.94023
- 6) -4.03587

### Exercise 3

Compute  $\int_5^9 \left( \frac{5625}{(-3 - 5t)^4} \right) dt$

- 1) -4.02019
- 2) -1.6843
- 3) -4.27411
- 4) 0.0136919
- 5)  $7.91979 \times 10^7$
- 6) -3.49169

## Exercise 4

Compute  $\int_5^6 \left( \frac{-5 + a - 5t - at}{-1 + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1)  $-0.154151$
- 2)  $-0.379551$
- 3)  $0.145049$
- 4) The rest of the solutions are not correct
- 5)  $-0.598351$
- 6)  $-0.901351$

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 3t^2 + t^3 + 2t^4 \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 70 millions of euros, compute the deposits available after 3 years.

- 1)  $\frac{3038}{5}$  millions of euros = 607.6 millions of euros
- 2)  $\frac{4289}{20}$  millions of euros = 214.45 millions of euros
- 3)  $\frac{1433}{20}$  millions of euros = 71.65 millions of euros
- 4)  $\frac{474}{5}$  millions of euros = 94.8 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = \sin(-4 + 8t) \text{ euros.}$$

Compute the average value of the shares along the first  $3\pi$  months of the year (between  $t=0$  and  $t=3\pi$ ).

- 1)  $-20$  euros
- 2)  $0$  euros
- 3)  $70$  euros
- 4)  $40$  euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -1 + x^2$  and the horizontal axis between the points  $x = -5$  and  $x = 0$ .

1)  $\frac{110}{3} = 36.6667$

2)  $\frac{79}{2} = 39.5$

3)  $\frac{85}{2} = 42.5$

4)  $\frac{81}{2} = 40.5$

5) 41

6) 38

7)  $\frac{83}{2} = 41.5$

8) 42

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \sin(-2 + 4t) \text{ per-unit.}$$

The initial deposit in the account is 17000 euros. Compute the deposit after  $3\pi$  years.

1) 16950 euros

2) 17000 euros

3) 17070 euros

4) 17040 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
20531650581

### Exercise 1

Compute  $\int_{-2a}^5 (4a + 4t - 12at - 9t^2 - 12at^2 - 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -631
- 2) The rest of the solutions are not correct
- 3) -630
- 4) -643
- 5) -639
- 6) -649

### Exercise 2

Compute  $\int_2^3 (e^{-1-2t} (4 + 4t)) dt$

- 1) -3.60903
- 2) -2.96293
- 3) -3.28584
- 4) -3.84426
- 5) -0.0804507
- 6) 0.0389587

### Exercise 3

Compute  $\int_{-9}^{-5} \left( \frac{64}{(-2 - 2t)^4} \right) dt$

- 1) -2.96293
- 2) -3.60903
- 3) 338 603.
- 4) 0.0182292
- 5) -3.28584
- 6) -3.84426



## Exercise 4

Compute  $\int_3^4 \left( \frac{6 + 8a + 3t - 4at}{-4 + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) -1.27899
- 2) The rest of the solutions are not correct
- 3) -1.33869
- 4) -1.37439
- 5) -0.729286
- 6) -0.817786

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (6 + t)(\sin(2\pi t) + 2) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 50 millions of euros, compute the deposits available after 5 years.

- 1)  $63 - \frac{1}{2\pi}$  millions of euros = 62.8408 millions of euros
- 2)  $39 + \frac{1}{2\pi}$  millions of euros = 39.1592 millions of euros
- 3)  $78 - \frac{1}{\pi}$  millions of euros = 77.6817 millions of euros
- 4)  $135 - \frac{5}{2\pi}$  millions of euros = 134.2042 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 20 e^{3+2t} \text{ euros.}$$

Compute the average value of the shares along the first 6 months of the year (between  $t=0$  and  $t=6$ ).

- 1)  $\frac{1}{6} (10 e - 10 e^3)$  euros = -28.9454 euros
- 2)  $\frac{1}{6} (-10 e^3 + 10 e^5)$  euros = 213.8794 euros
- 3)  $\frac{1}{6} (-10 e^3 + 10 e^7)$  euros = 1794.246 euros
- 4)  $\frac{1}{6} (-10 e^3 + 10 e^{15})$  euros =  $5.4483 \times 10^6$  euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 8 - 2x^2$  and the horizontal axis between the points  $x=-2$  and  $x=4$ .

1)  $\frac{137}{3} = 45.6667$

2)  $\frac{271}{6} = 45.1667$

3)  $\frac{265}{6} = 44.1667$

4)  $\frac{128}{3} = 42.6667$

5) 0

6)  $\frac{140}{3} = 46.6667$

7)  $\frac{134}{3} = 44.6667$

8)  $\frac{283}{6} = 47.1667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{12} e^{-6+3t} \text{ per-unit.}$$

The initial deposit in the account is 15000 euros. Compute the deposit after 2 years.

1) 15481.4458 euros

2) 15501.4458 euros

3) 15471.4458 euros

4) 15421.4458 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
20705551589

### Exercise 1

Compute  $\int_{3a}^3 (18a - 12t + 66at - 33t^2 + 36at^2 - 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) -91
- 3) -86
- 4) -97
- 5) -100
- 6) -85

### Exercise 2

Compute  $\int_{-3}^3 (-2 \cos[t]) dt$

- 1) 11.8799
- 2) -4.77604
- 3) -4.21642
- 4) 0.
- 5) -0.56448
- 6) -4.20154

### Exercise 3

Compute  $\int_{-7}^{-3} \left(\frac{9}{t^5}\right) dt$

- 1) 29230.
- 2) -2.77019
- 3) -4.20154
- 4) -4.21642
- 5) -4.77604
- 6) -0.0268407

## Exercise 4

Compute  $\int_0^1 \left( \frac{-2 - 8a - 2t - 4at}{2 + 3t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2)  $-3.61429$
- 3)  $-3.51219$
- 4)  $-2.00629$
- 5)  $-2.11539$
- 6)  $-2.64609$

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (3 + 3t)(\sin(2\pi t) + 1) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was  $60$  millions of euros, compute the deposits available after  $5$  years.

- 1)  $\frac{117}{2} + \frac{3}{2\pi}$  millions of euros =  $58.9775$  millions of euros
- 2)  $\frac{225}{2} - \frac{15}{2\pi}$  millions of euros =  $110.1127$  millions of euros
- 3)  $72 - \frac{3}{\pi}$  millions of euros =  $71.0451$  millions of euros
- 4)  $\frac{129}{2} - \frac{3}{2\pi}$  millions of euros =  $64.0225$  millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = \cos(2t) \text{ euros.}$$

Compute the average value of the shares along the first  $\pi$  months of the year (between  $t=0$  and  $t=\pi$ ).

- 1)  $70$  euros
- 2)  $-20$  euros
- 3)  $0$  euros
- 4)  $80$  euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -12 - 14x + 2x^3$  and the horizontal axis between the points  $x = -5$  and  $x = 1$ .

- 1) 171
- 2)  $\frac{441}{2} = 220.5$
- 3) 219
- 4) 221
- 5) 216
- 6) 222
- 7) 168
- 8)  $\frac{443}{2} = 221.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \cos(5 + 3t) \text{ per-unit.}$$

The initial deposit in the account is 8000 euros. Compute the deposit after  $2\pi$  years.

- 1) 8090 euros
- 2) 7950 euros
- 3) 8000 euros
- 4) 8030 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
20714551324

### Exercise 1

Compute  $\int_{3a}^2 (-6 - 3a + 2t - 54at + 27t^2 + 36at^2 - 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) 4
- 2) 2
- 3) The rest of the solutions are not correct
- 4)  $\emptyset$
- 5) -18
- 6) -12

### Exercise 2

Compute  $\int_2^3 (-2 \cos[t]) dt$

- 1) -5.15814
- 2) -5.23793
- 3) 4.27537
- 4) 1.53635
- 5) 2.79047
- 6) -7.39363

### Exercise 3

Compute  $\int_{-8}^{-5} \left(\frac{8}{t}\right) dt$

- 1) -3.76003
- 2) -0.470004
- 3) -12.8191
- 4) -12.6239
- 5) -18.095
- 6) -12.3667

## Exercise 4

Compute  $\int_2^4 \left( \frac{2 + 8a + 2t + 4at}{2 + 3t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) 1.9795
- 2) 1.1626
- 3) 2.0433
- 4) 1.0464
- 5) 2.1669
- 6) The rest of the solutions are not correct

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (8 + 6t)(\cos(2\pi t) + 2) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 60 millions of euros, compute the deposits available after 5 years.

- 1) 290 millions of euros
- 2) 50 millions of euros
- 3) 116 millions of euros
- 4) 82 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = \cos(-8 + 7t) \text{ euros.}$$

Compute the average value of the shares along the first  $3\pi$  months of the year (between  $t=0$  and  $t=3\pi$ ).

- 1)  $80 + \frac{2 \sin[8]}{21\pi}$  euros = 80.03 euros
- 2)  $60 + \frac{2 \sin[8]}{21\pi}$  euros = 60.03 euros
- 3)  $\frac{2 \sin[8]}{21\pi}$  euros = 0.03 euros
- 4)  $90 + \frac{2 \sin[8]}{21\pi}$  euros = 90.03 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -12 - 14x + 2x^3$  and the horizontal axis between the points  $x = -5$  and  $x = 0$ .

- 1) 203
- 2)  $\frac{395}{2} = 197.5$
- 3)  $\frac{405}{2} = 202.5$
- 4)  $\frac{407}{2} = 203.5$
- 5)  $\frac{373}{2} = 186.5$
- 6) 202
- 7)  $\frac{401}{2} = 200.5$
- 8)  $\frac{379}{2} = 189.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \cos(4 + 8t) \text{ per-unit.}$$

The initial deposit in the account is 8000 euros. Compute the deposit after  $4\pi$  years.

- 1) 7970 euros
- 2) 8000 euros
- 3) 8050 euros
- 4) 8007.901 euros



## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
20730551515

### Exercise 1

Compute  $\int_a^1 (-6a + 12t - 14at + 21t^2 + 9at^2 - 12t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -14
- 2) -13
- 3) -10
- 4) -3
- 5) -1
- 6) The rest of the solutions are not correct

### Exercise 2

Compute  $\int_{-1}^2 (\sin[3 + t]) dt$

- 1) -0.699809
- 2) -2.95518
- 3) -3.13767
- 4) -1.00855
- 5) -2.83255
- 6) -0.151178

### Exercise 3

Compute  $\int_{-6}^{-2} \left( \frac{768}{(-2 + 4t)^4} \right) dt$

- 1) -2.95518
- 2) 0.0603587
- 3) -3.13767
- 4)  $-3.92713 \times 10^6$
- 5) -2.2437
- 6) -2.83255

### Exercise 4

Compute  $\int_2^4 \left( \frac{3 + a - 3t + at}{-1 + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) 0.973412
- 3) 0.711212
- 4) 1.07341
- 5) 1.09861
- 6) 0.435612

### Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = 2 + 2t + 3t^3 \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 40 millions of euros, compute the deposits available after 2 years.

- 1) 256 millions of euros
- 2)  $\frac{175}{4}$  millions of euros = 43.75 millions of euros
- 3) 60 millions of euros
- 4)  $\frac{463}{4}$  millions of euros = 115.75 millions of euros

### Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (-7 + 8t) \sin(6t) \text{ euros.}$$

Compute the average value of the shares along the first  $\pi$  months of the year (between  $t=0$  and  $t=\pi$ ).

- 1) -4 euros
- 2)  $\frac{4}{3}$  euros = 1.3333 euros
- 3)  $-\frac{8}{3}$  euros = -2.6667 euros
- 4)  $-\frac{4}{3}$  euros = -1.3333 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 1 - x^2$  and the horizontal axis between the points  $x=-1$  and  $x=5$ .

1)  $\frac{253}{6} = 42.1667$

2)  $\frac{247}{6} = 41.1667$

3)  $\frac{128}{3} = 42.6667$

4)  $\frac{122}{3} = 40.6667$

5) 36

6)  $\frac{116}{3} = 38.6667$

7)  $\frac{125}{3} = 41.6667$

8)  $\frac{241}{6} = 40.1667$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{1}{100} (8 - 8t)\right) \sin(2t) \text{ per-unit.}$$

The initial deposit in the account is 5000 euros. Compute the deposit after  $4\pi$  years.

1) 8256.7551 euros

2) 8295.5208 euros

3) 8265.5208 euros

4) 8205.5208 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
20902651249

## Exercise 1

Compute  $\int_{-3a}^5 (-9 + 9a + 6t + 36at + 18t^2 - 18at^2 - 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -276
- 2) -283
- 3) The rest of the solutions are not correct
- 4) -282
- 5) -272
- 6) -296

## Exercise 2

Compute  $\int_{-2}^3 ((-6 + 6t) \cos[1 + 2t]) dt$

- 1) 30.5449
- 2) -16.3524
- 3) -21.1282
- 4) 5.28768
- 5) -25.5676
- 6) -15.1273

## Exercise 3

Compute  $\int_1^2 \left(\frac{5}{t^4}\right) dt$

- 1) 1.45833
- 2) -5.82712
- 3) -7.05151
- 4) -4.17209
- 5) -4.50998
- 6) 330.667

## Exercise 4

Compute  $\int_5^6 \left( \frac{-10 + 9a - 5t - 3at}{-6 - t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) The rest of the solutions are not correct
- 2) -1.02389
- 3) -0.915494
- 4) -1.34619
- 5) -1.38049
- 6) -0.400594

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (2 + t)e^{3+3t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 50 millions of euros, compute the deposits available after 2 years.

- 1)  $50 - \frac{5e^3}{9} + \frac{11e^9}{9}$  millions of euros = 9942.6106 millions of euros
- 2)  $50 - \frac{5e^3}{9} + \frac{8e^6}{9}$  millions of euros = 397.4447 millions of euros
- 3)  $\frac{452}{9} - \frac{5e^3}{9}$  millions of euros = 39.0636 millions of euros
- 4)  $50 - \frac{5e^3}{9} + \frac{14e^{12}}{9}$  millions of euros = 253212.9614 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month t:

$$V(t) = 20e^{-1+t} \text{ euros.}$$

Compute the average value of the shares along the first 8 months of the year (between t=0 and t=8).

- 1)  $\frac{1}{8} \left( \frac{20}{e^2} - \frac{20}{e} \right)$  euros = -0.5814 euros
- 2)  $\frac{1}{8} \left( -\frac{20}{e} + 20e^7 \right)$  euros = 2740.6632 euros
- 3)  $\frac{1}{8} \left( -\frac{20}{e} + 20e \right)$  euros = 5.876 euros
- 4)  $\frac{1}{8} \left( 20 - \frac{20}{e} \right)$  euros = 1.5803 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 12x + 2x^2 - 2x^3$  and the horizontal axis between the points  $x = -5$  and  $x = 1$ .

- 1) 252
- 2)  $\frac{826}{3} = 275.3333$
- 3)  $\frac{719}{3} = 239.6667$
- 4)  $\frac{820}{3} = 273.3333$
- 5) 261
- 6)  $\frac{1649}{6} = 274.8333$
- 7)  $\frac{1655}{6} = 275.8333$
- 8)  $\frac{829}{3} = 276.3333$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{13} e^{-6+2t} \text{ per-unit.}$$

The initial deposit in the account is 12000 euros. Compute the deposit after 3 years.

- 1) 12529.3403 euros
- 2) 12509.3403 euros
- 3) 12469.3403 euros
- 4) 12449.3403 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
21104501336

### Exercise 1

Compute  $\int_{-2a}^1 (-2 + 14a + 14t - 28at - 21t^2 + 12at^2 + 8t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -53
- 2) The rest of the solutions are not correct
- 3) -30
- 4) -36
- 5) -48
- 6) -47

### Exercise 2

Compute  $\int_0^3 (e^{2-3t} (-6 - 6t)) dt$

- 1) -78.5191
- 2) -98.3279
- 3) -19.6962
- 4) -0.0410347
- 5) 0.0136782
- 6) -71.4916

### Exercise 3

Compute  $\int_3^6 \left(-\frac{384}{(5-4t)^3}\right) dt$

- 1) -63960.
- 2) -3.54955
- 3) -3.62971
- 4) -4.99222
- 5) 0.846628
- 6) -3.9865

## Exercise 4

Compute  $\int_0^1 \left( \frac{9 + 8a + 3t + 4at}{6 + 5t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) 0.735428
- 2) 1.16173
- 3) The rest of the solutions are not correct
- 4) 0.891928
- 5) 0.878728
- 6) 1.15073

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (6 + 8t)(\cos(2\pi t) + 2) \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 30 millions of euros, compute the deposits available after 4 years.

- 1) 26 millions of euros
- 2) 86 millions of euros
- 3) 206 millions of euros
- 4) 50 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 2 + 2t + t^2 + t^3 + 3t^4 \text{ euros.}$$

Compute the average value of the shares along the first 6 months of the year (between  $t=0$  and  $t=6$ ).

- 1)  $\frac{4258}{5}$  euros = 851.6 euros
- 2)  $\frac{254}{45}$  euros = 5.6444 euros
- 3)  $\frac{251}{360}$  euros = 0.6972 euros
- 4)  $\frac{1267}{40}$  euros = 31.675 euros



## Exercise 7

Compute the area enclosed by the function  $f(x) = 18 + 15x + 3x^2$  and the horizontal axis between the points  $x=2$  and  $x=5$ .

- 1)  $\frac{665}{2} = 332.5$
- 2)  $\frac{667}{2} = 333.5$
- 3) 330
- 4) 332
- 5)  $\frac{661}{2} = 330.5$
- 6)  $\frac{657}{2} = 328.5$
- 7)  $\frac{663}{2} = 331.5$
- 8) 331

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{100} \text{ per-unit.}$$

The initial deposit in the account is 20000 euros. Compute the deposit after 2 years.

- 1) 20454.0268 euros
- 2) 20404.0268 euros
- 3) 20424.0268 euros
- 4) 20414.0268 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
21130550766

### Exercise 1

Compute  $\int_{3a}^2 (2 - 33a + 22t + 18at - 9t^2 + 36at^2 - 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) 55
- 2) 62
- 3) The rest of the solutions are not correct
- 4) 48
- 5) 44
- 6) 60

### Exercise 2

Compute  $\int_1^2 (-2t \cos[2-t]) dt$

- 1) -11.9125
- 2) -11.4644
- 3) -11.639
- 4) -2.60234
- 5) -11.4894
- 6) -0.841471

### Exercise 3

Compute  $\int_{-2}^{-1} \left(-\frac{3}{(1-t)^3}\right) dt$

- 1) -4.40543
- 2) -4.47253
- 3) -4.57761
- 4) -4.41505
- 5) 32.5
- 6) -0.208333

## Exercise 4

Compute  $\int_2^4 \left( \frac{-2 + 6a - 2t + 3at}{2 + 3t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) 1.23928
- 2) 1.41938
- 3) 1.53248
- 4) 1.43278
- 5) The rest of the solutions are not correct
- 6) 0.978477

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (6 + 6t)e^{-2+2t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 60 millions of euros, compute the deposits available after 2 years.

- 1)  $\frac{129}{2} - \frac{3}{2e^2}$  millions of euros = 64.297 millions of euros
- 2)  $60 - \frac{3}{2e^4} - \frac{3}{2e^2}$  millions of euros = 59.7695 millions of euros
- 3)  $60 - \frac{3}{2e^2} + \frac{15e^2}{2}$  millions of euros = 115.2149 millions of euros
- 4)  $60 - \frac{3}{2e^2} + \frac{21e^4}{2}$  millions of euros = 633.0776 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = \cos(-2 + 3t) \text{ euros.}$$

Compute the average value of the shares along the first  $\pi$  months of the year (between  $t=0$  and  $t=\pi$ ).

- 1)  $40 + \frac{2 \sin[2]}{3\pi}$  euros = 40.193 euros
- 2)  $30 + \frac{2 \sin[2]}{3\pi}$  euros = 30.193 euros
- 3)  $90 + \frac{2 \sin[2]}{3\pi}$  euros = 90.193 euros
- 4)  $\frac{2 \sin[2]}{3\pi}$  euros = 0.193 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = -4 - 2x + 4x^2 + 2x^3$  and the horizontal axis between the points  $x = -3$  and  $x = 4$ .

1)  $\frac{1043}{6} = 173.8333$

2)  $\frac{598}{3} = 199.3333$

3)  $\frac{1199}{6} = 199.8333$

4)  $\frac{1181}{6} = 196.8333$

5)  $\frac{595}{3} = 198.3333$

6)  $\frac{1117}{6} = 186.1667$

7)  $\frac{1193}{6} = 198.8333$

8)  $\frac{369}{2} = 184.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{10} \cos(-2 + 5t) \text{ per-unit.}$$

The initial deposit in the account is 7000 euros. Compute the deposit after  $4\pi$  years.

1) 7030 euros

2) 7040 euros

3) 7090 euros

4) 7000 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
30216550613

### Exercise 1

Compute  $\int_{2a}^5 (3 - 14a + 14t + 4at - 3t^2 + 6at^2 - 4t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -149
- 2) -151
- 3) -156
- 4) The rest of the solutions are not correct
- 5) -136
- 6) -134

### Exercise 2

Compute  $\int_3^6 ((3 - t) \text{Log}[t]) dt$

- 1) -1.33127
- 2) -24.1344
- 3) -7.19376
- 4) -4.94376
- 5) -25.1432
- 6) -32.8728

### Exercise 3

Compute  $\int_{-2}^0 \left( \frac{729}{(3 - 3t)^4} \right) dt$

- 1) 19 602.
- 2) -6.04435
- 3) 2.88889
- 4) -13.2011
- 5) -9.69195
- 6) -10.0971

## Exercise 4

Compute  $\int_4^6 \left( \frac{2 + 3a - t + 3at}{-2 - t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter  $a$ .  
Compute the derivative of such a formula at the point  $0$ .

- 1) The rest of the solutions are not correct
- 2) 2.76844
- 3) 2.97264
- 4) 1.64904
- 5) 2.07944
- 6) 1.86754

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (8 + 5t)e^{1+t} \text{ millions of euros/year.}$$

If the initial deposit in the investment fund was 70 millions of euros, compute the deposits available after 1 year.

- 1)  $70 - 3e + 13e^3$  millions of euros = 322.9571 millions of euros
- 2)  $68 - 3e$  millions of euros = 59.8452 millions of euros
- 3)  $70 - 3e + 18e^4$  millions of euros = 1044.6119 millions of euros
- 4)  $70 - 3e + 8e^2$  millions of euros = 120.9576 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (4 + 3t)(\sin(2\pi t) + 1) \text{ euros.}$$

Compute the average value of the shares along the first 6 months of the year (between  $t=0$  and  $t=6$ ).

- 1)  $\frac{1}{6} \left( -\frac{5}{2} + \frac{3}{2\pi} \right)$  euros = -0.3371 euros
- 2)  $\frac{1}{6} \left( 14 - \frac{3}{\pi} \right)$  euros = 2.1742 euros
- 3)  $\frac{1}{6} \left( \frac{11}{2} - \frac{3}{2\pi} \right)$  euros = 0.8371 euros
- 4)  $\frac{1}{6} \left( 78 - \frac{9}{\pi} \right)$  euros = 12.5225 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 6 + 3x - 3x^2$  and the horizontal axis between the points  $x=-1$  and  $x=4$ .

1)  $\frac{79}{2} = 39.5$

2)  $\frac{91}{2} = 45.5$

3)  $\frac{89}{2} = 44.5$

4)  $\frac{25}{2} = 12.5$

5)  $\frac{85}{2} = 42.5$

6)  $\frac{83}{2} = 41.5$

7) 42

8)  $\frac{87}{2} = 43.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left( \frac{1}{100} (4 + 3t) \right) (\sin(2\pi t) + 1) \text{ per-unit.}$$

The initial deposit in the account is 5000 euros. Compute the deposit after 5 years.

1) 8746.0354 euros

2) 8756.0354 euros

3) 8676.0354 euros

4) 8716.0354 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
30312650522

### Exercise 1

Compute  $\int_{3a}^{\theta} (-3 + 24a - 16t + 6at - 3t^2 - 36at^2 + 16t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) 25
- 2) -10
- 3) The rest of the solutions are not correct
- 4) 14
- 5) 1
- 6) 9

### Exercise 2

Compute  $\int_{-2}^2 ((-3 + 3t) \sin[2 + t]) dt$

- 1) 12.
- 2) -38.0145
- 3) -34.1604
- 4) -27.4375
- 5) 0.
- 6) -9.30948

### Exercise 3

Compute  $\int_3^4 \left( \frac{2\theta}{-3 + 4t} \right) dt$

- 1) 0.367725
- 2) -6.74669
- 3) -7.50787
- 4) -5.41892
- 5) -5.09906
- 6) 1.83862



## Exercise 4

Compute  $\int_4^5 \left( \frac{-3 - 15a + 3t + 5at}{3 - 4t + t^2} \right) dt$

- . The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) 1.43841
- 2) 0.48241
- 3) 2.07681
- 4) The rest of the solutions are not correct
- 5) 1.49041
- 6) 1.12431

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (1 + t + 3t^2) \log(3t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 70 millions euros, compute the deposit available after (with respect to  $t=1$ ) 4 years.

- 1)  $\frac{169}{4} - \frac{5 \text{Log}[3]}{2} + 76 \text{Log}[12]$  millions of euros = 228.3564 millions of euros
- 2)  $\frac{236}{3} - \frac{5 \text{Log}[3]}{2} + \frac{285 \text{Log}[15]}{2}$  millions of euros = 461.8173 millions of euros
- 3)  $-\frac{185}{12} - \frac{5 \text{Log}[3]}{2} + 240 \text{Log}[18]$  millions of euros = 675.526 millions of euros
- 4)  $\frac{56}{3} - \frac{5 \text{Log}[3]}{2} + \frac{285 \text{Log}[15]}{2}$  millions of euros = 401.8173 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = (-3 - 4t) \cos(3t) \text{ euros.}$$

Compute the average value of the shares along the first  $3\pi$  months of the year (between  $t=0$  and  $t=3\pi$ ).

- 1)  $\frac{8}{27\pi}$  euros = 0.0943 euros
- 2) 0 euros
- 3)  $20 + \frac{8}{27\pi}$  euros = 20.0943 euros
- 4)  $50 + \frac{8}{27\pi}$  euros = 50.0943 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 6 - 5x - 2x^2 + x^3$  and the horizontal axis between the points  $x=0$  and  $x=5$ .

- 1)  $\frac{643}{12} = 53.5833$
- 2)  $\frac{485}{12} = 40.4167$
- 3)  $\frac{613}{12} = 51.0833$
- 4)  $\frac{637}{12} = 53.0833$
- 5)  $\frac{137}{4} = 34.25$
- 6)  $\frac{631}{12} = 52.5833$
- 7)  $\frac{649}{12} = 54.0833$
- 8)  $\frac{655}{12} = 54.5833$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \left(\frac{1}{100} (3 - 2t)\right) \cos(6t) \text{ per-unit.}$$

The initial deposit in the account is 20000 euros. Compute the deposit after  $4\pi$  years.

- 1) 19990 euros
- 2) 20050 euros
- 3) 19970 euros
- 4) 20000 euros

## Mathematics 1 - ADE/FyCo - 2020/2021

List of exercises 03-Integration for identity number:  
30509500045

### Exercise 1

Compute  $\int_{3a}^5 (1 - 9a + 6t + 6at - 3t^2 + 27at^2 - 12t^3) dt$

. The resulting expression is a formula in terms of parameter  $a$ . Compute the derivative of such a formula at the point  $\theta$ .

- 1) -1014
- 2) The rest of the solutions are not correct
- 3) -1008
- 4) -998
- 5) -996
- 6) -1003

### Exercise 2

Compute  $\int_{-3}^2 (-2 \cos[1 - 2t]) dt$

- 1) -4.62338
- 2) 1.68872
- 3) -4.93629
- 4) -0.798107
- 5) -0.563444
- 6) -4.14798

### Exercise 3

Compute  $\int_4^8 \left( \frac{3}{(1-t)^4} \right) dt$

- 1) -4.93629
- 2) -3.49029
- 3) -4.62338
- 4) 5521.33
- 5) 0.0341216
- 6) -4.14798

## Exercise 4

Compute  $\int_{-1}^0 \left( \frac{-10 - 15a - 5t - 5at}{6 + 5t + t^2} \right) dt$

. The resulting expression is a formula in terms of parameter a. Compute the derivative of such a formula at the point 0.

- 1) -3.28854
- 2) -3.92794
- 3) -3.46574
- 4) The rest of the solutions are not correct
- 5) -3.72094
- 6) -4.22244

## Exercise 5

The deposits of an investment fund vary from one year to another being the speed of that variation determined by the function

$$v(t) = (4 + t + 3t^2) \log(5t) \text{ millions of euros/year.}$$

If, for  $t=1$ , the deposits in the investment fund were 60 millions euros, compute the deposit available after (with respect to  $t=1$ ) 5 years.

- 1)  $-\frac{10}{3} - \frac{11 \log[5]}{2} + \frac{315 \log[25]}{2}$  millions of euros = 494.7877 millions of euros
- 2)  $\frac{235}{12} - \frac{11 \log[5]}{2} + 258 \log[30]$  millions of euros = 888.2403 millions of euros
- 3)  $-\frac{485}{12} - \frac{11 \log[5]}{2} + 258 \log[30]$  millions of euros = 828.2403 millions of euros
- 4)  $\frac{93}{4} - \frac{11 \log[5]}{2} + 88 \log[20]$  millions of euros = 278.0225 millions of euros

## Exercise 6

The true value of certain shares oscillates along the year.

The following function yields the value of the shares for each month  $t$ :

$$V(t) = 30 e^{2+t} \text{ euros.}$$

Compute the average value of the shares along the first 8 months of the year (between  $t=0$  and  $t=8$ ).

- 1)  $\frac{1}{8} (30 e - 30 e^2)$  euros = -17.5154 euros
- 2)  $\frac{1}{8} (-30 e^2 + 30 e^3)$  euros = 47.6118 euros
- 3)  $\frac{1}{8} (-30 e^2 + 30 e^{10})$  euros = 82571.5378 euros
- 4)  $\frac{1}{8} (-30 e^2 + 30 e^4)$  euros = 177.0341 euros

## Exercise 7

Compute the area enclosed by the function  $f(x) = 24 + 8x - 6x^2 - 2x^3$  and the horizontal axis between the points  $x=0$  and  $x=3$ .

- 1) 69
- 2) 68
- 3)  $\frac{141}{2} = 70.5$
- 4)  $\frac{133}{2} = 66.5$
- 5)  $\frac{139}{2} = 69.5$
- 6) 70
- 7)  $\frac{137}{2} = 68.5$
- 8)  $\frac{27}{2} = 13.5$

## Exercise 8

Certain bank account offers a variable continuous compound interest rate. The interest rate for each year is given by the function

$$I(t) = \frac{1}{15} e^{-6 \cdot 2^t} \text{ per-unit.}$$

The initial deposit in the account is 5000 euros. Compute the deposit after 3 years.

- 1) 5149.0485 euros
- 2) 5249.0485 euros
- 3) 5190.2828 euros
- 4) 5169.0485 euros